



Balanced Field Length Calculation for a Learjet 35A/36A with Under-Wing Stores on a Wet Runway

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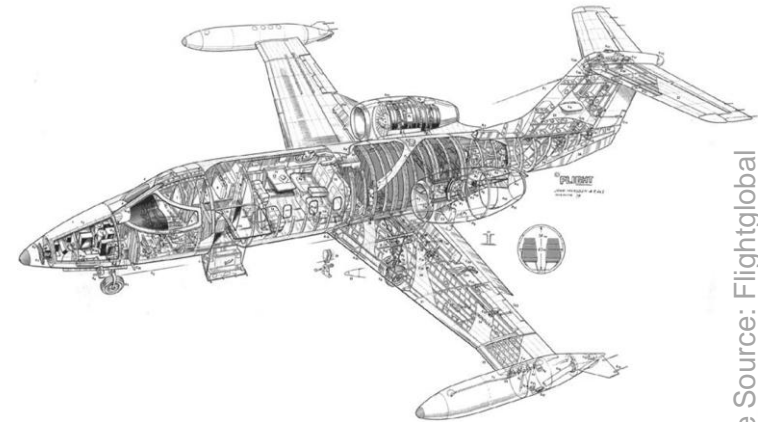
In Cooperation with GFD mbH and Aero Group



HAW Hamburg, 31.08.2012

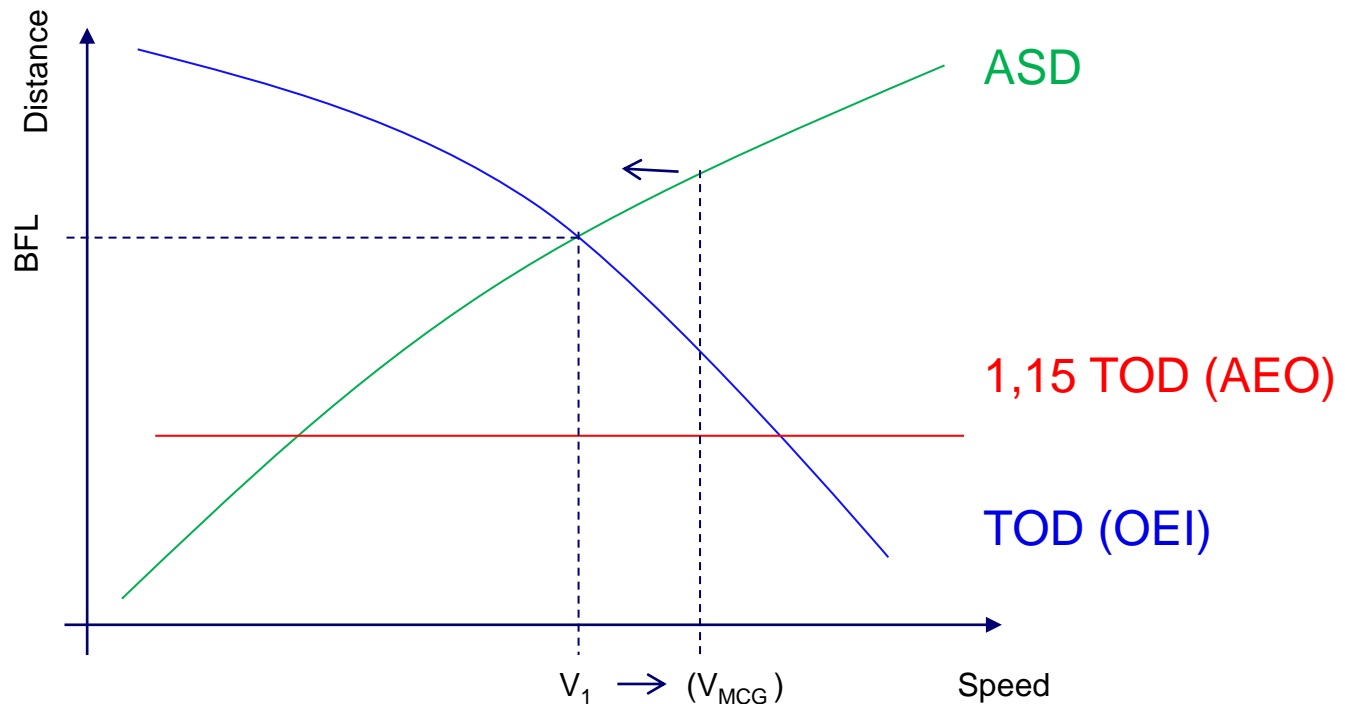
Structure of the Presentation

- **Introduction**
 - Takeoff and Balanced Field Length
 - Learjet 35A/36A with Under-Wing Stores, Existing Takeoff Operation Envelope
- **Calculation Approach**
 - Equation of Motion and Possible Calculation Approaches
 - Calibration Concept and Simulation Architecture
- **Parameters and Forces**
 - Main Flight Mechanical Parameters
 - Impingement Spray Drag Force
- **Simulation Results**
 - Simulation Output and Calibration
 - Integration into Existing Data Set and Relations
 - Result Plausibility and Variation Effects
- **Conclusions**
 - Main Conclusions from Results
 - Additional Benefits of Numerical Simulation
 - Résumé

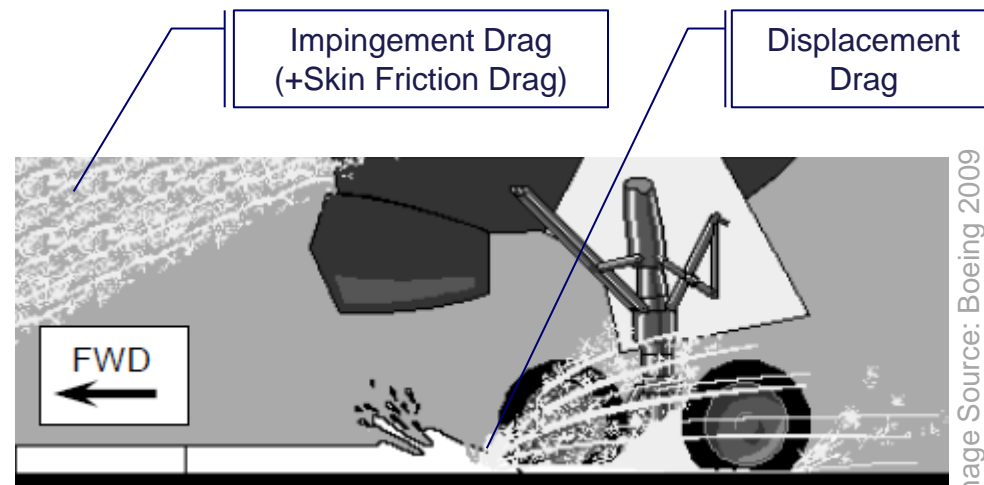


Introduction

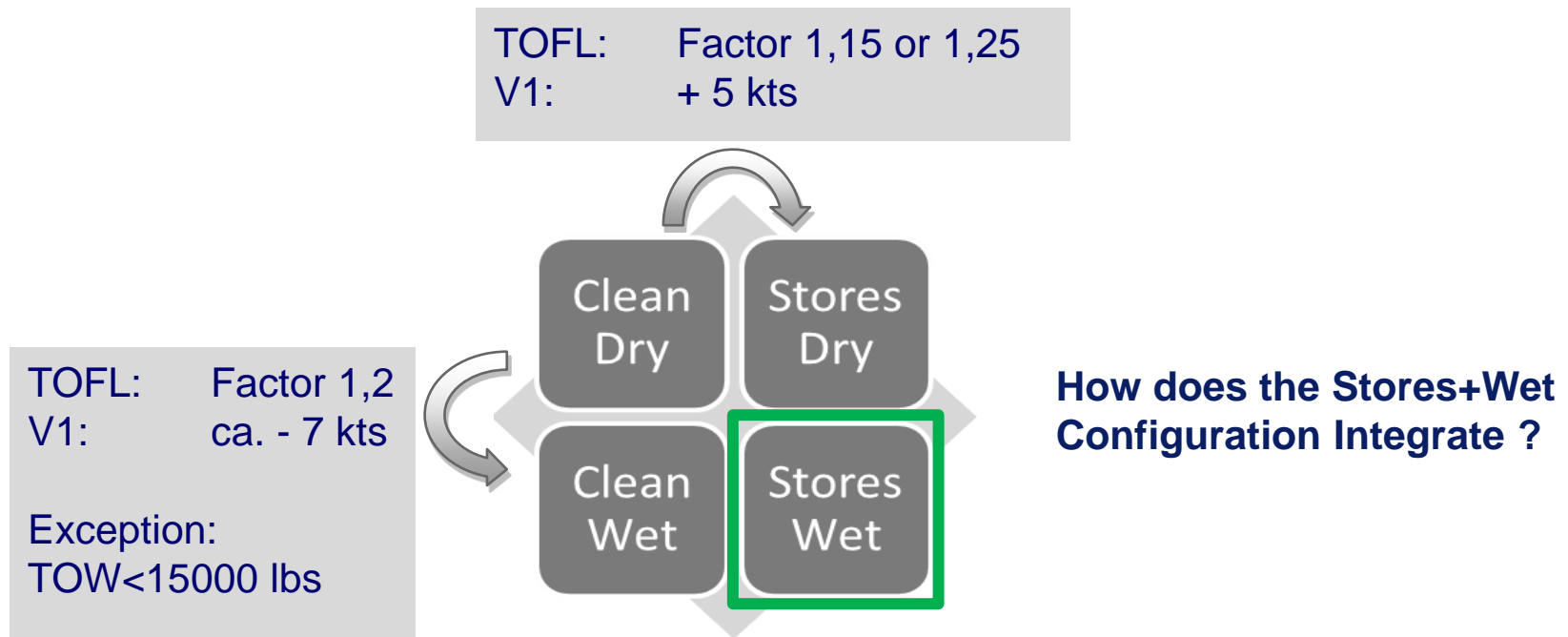
- **Balanced Field Length: Takeoff Distance + Accelerate-Stop Distance equal**
- **Decision Speed V_1 is transition between Stop+Go Decision (min. V_{MCG})**
- **Takeoff Field Length: Larger of Balanced Field Length and AEO Takeoff Dist.**



- Learjet 35A/36A operated by GFD with Under-Wing Stores
- Currently no takeoff operations permitted for Stores+Wet Runway Conditions
- Wet Runway: Braking Coefficient Reduction
Precipitation Drag Increment
Screen Height Reduction



- **4-Corner-Sheet Concept – Existing and New Configuration Performance Data**
- **Based on AFMS 9702-2 (Extended Tip Tanks), Wet Data Addendum**
- **Standard Corrections for Transition between Conditions and Configurations**



Calculation Approach

- Equation of Motion for Acceleration on Ground

$$S_G = m \cdot \int_0^{v_{LOF}} \frac{v_G}{T - D - F_f - m \cdot g \cdot \sin \gamma} dv_G$$

- Two different Solution Approaches possible

Used for Simulation

Used in AFMS-9702-2 Reference

Iterative Time-Step Wise Integration

- All Forces considered speed dependently
- Time-Step Wise Actions considered
- Close to Physical Reality
- Higher Accuracy

Average Speed Method

- All Forces averaged at $0,707 V_{LOF}$
- Average OEI Drag Coefficients
- Easier, simplified Calculation
- Result Precision limited

Introduction

Calculation Approach

Parameters and Forces

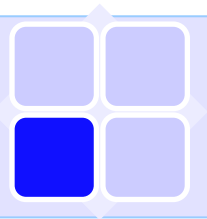
Simulation Results

Conclusions

Simulation Architecture to compare Simulation Results to AFMS Reference

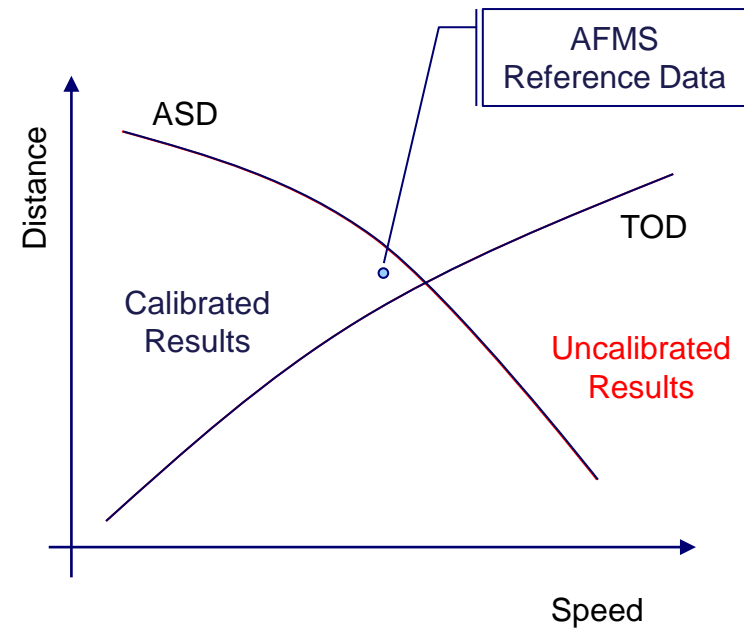
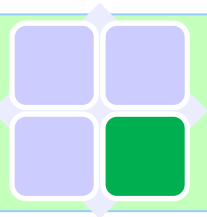
Calculation for Clean+Wet

- Determination of Calibration Factors



Calculation for Stores+Wet

- Determination of Simulation Results
- Determination of Calibrated Results



Parameters and Forces

- **Thrust**

$T_0 = 3400$ lbs (Installed)

- Variation with M, PA
- Variation with OAT
- Installation Loss 3%
- Flat Rating Characteristics
- Calibration with limited Engine Test Data

- **Lift Coefficient**

$C_{L,G} = 0,241$

- Lift Curve Slope Wing
- Zero Lift Angle Change with Wing Twist
- Flap Lift Increment
- Zero Lift Angle Change with Flaps
- Fuselage Lift Carryover
- Lift depletion after Spoiler Extension

- **Runway Friction Coefficient**

- Speed Dependent Rolling Friction Coefficient
- Braking Coefficient CS-25.109, Anti-Skid ON
- Max. Brake Energy Chart (Dry)
- Gear Load Factor (Braking Case)

- **Drag Coefficient**

$C_{D,TO,AEO} = 0,0606$

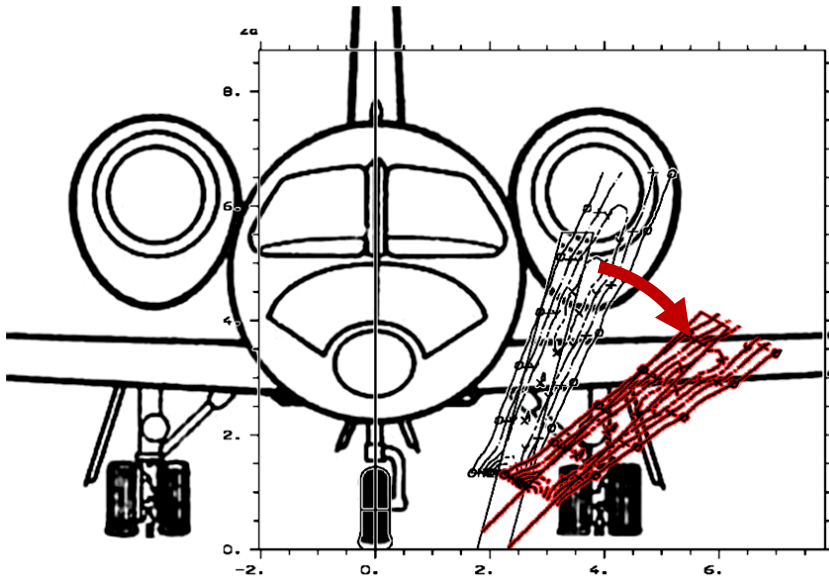
$C_{D,TO,OEI} = 0,0797$

- Equivalent Skin Friction Drag Coefficient, Learjet Wetted Areas determined at Aero, HAW
- Induced Drag with Oswald Efficiency Factor Estimation based on Literature Values
- Flap Drag Coefficient Increment
- Gear Drag Coefficient Increment
- Store Drag Coefficient Increment
- Spoiler Drag Coefficient Increment
- Windmilling Drag
- Asymmetrical Flight Condition Drag

Water Spray Drag

- Subject to intensive investigation
- Equation developed on the base of Water Mass Flow (NLR/NASA-inspired)

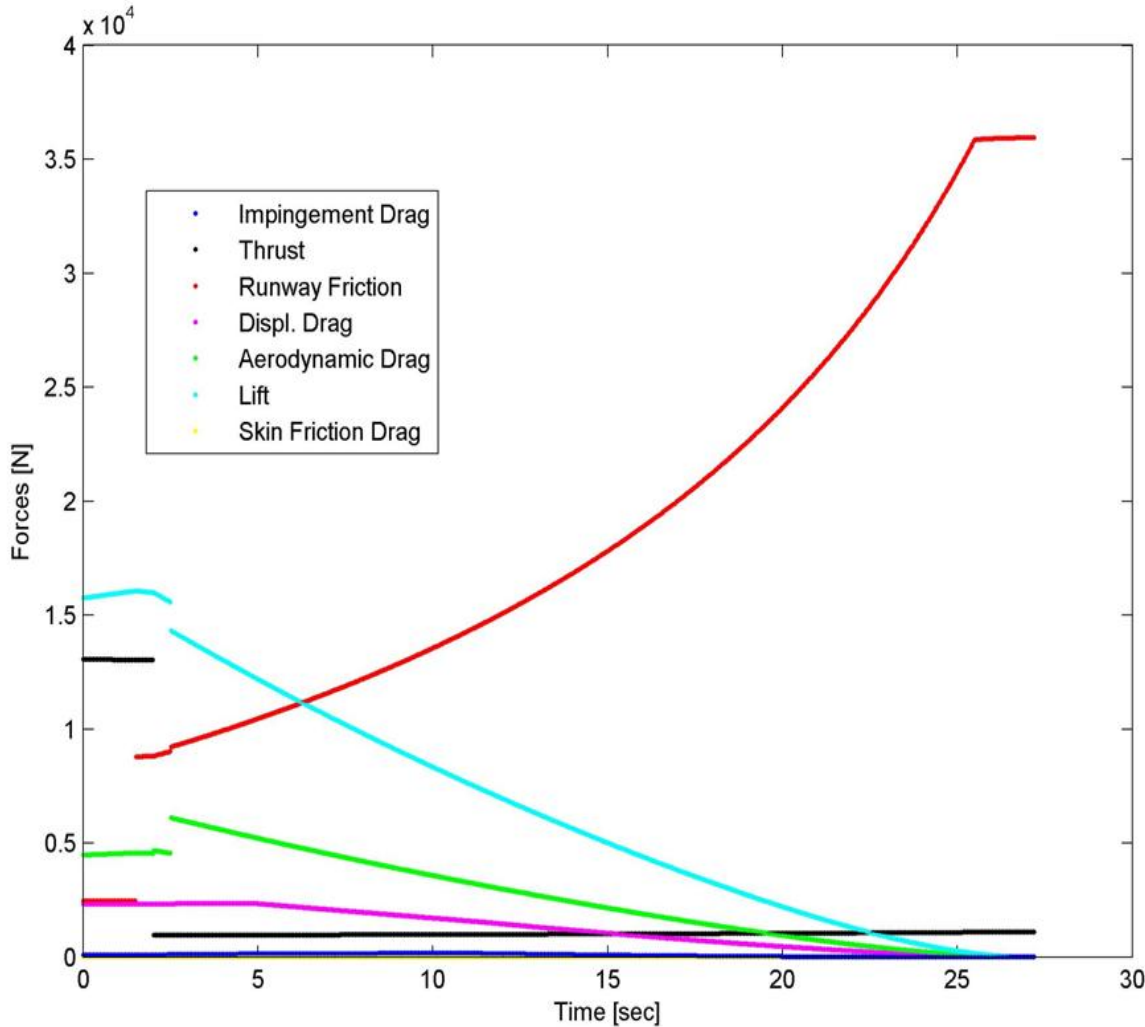
$$D_{imp} = k_{angle} \cdot 2 \dot{m}_{imp,semi} \cdot (1 - e_{res}) \cdot v_{aircraft}$$



- Spray Drag Maximum (Worst Case)

$$D_{imp} = 164 \text{ N}$$

For Comparison: $T_0 = 13451 \text{ N}$



Forces Variation with Time after Engine Failure (Simulation Result)

• Excess Thrust Balance

- Dominating: Thrust, Drag, Friction and Displacement Drag
- Negligible: Skin Friction and Impingement Drag

• Time Step Wise Effects

- Time Dependent Retardation Device Activation
- Increase in Braking Friction after Spoiler Activation

• Conclusion

- Store Installation critical through Aerodynamic Drag Increment
- Precipitation Effects at 3 mm water depth: only Displ. Drag



Introduction

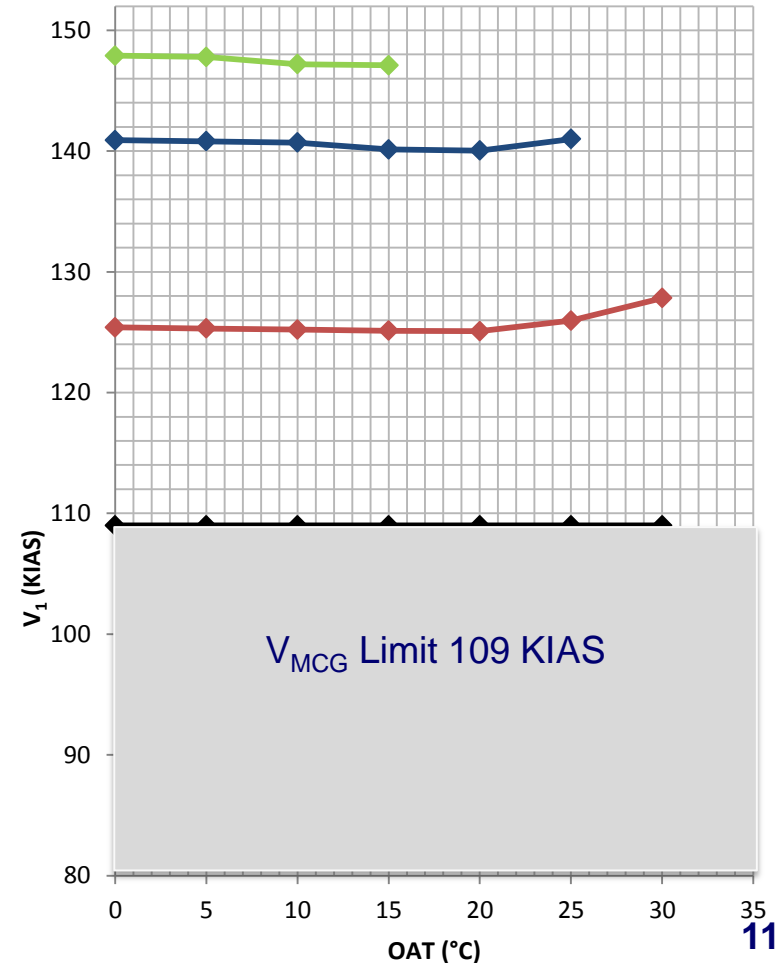
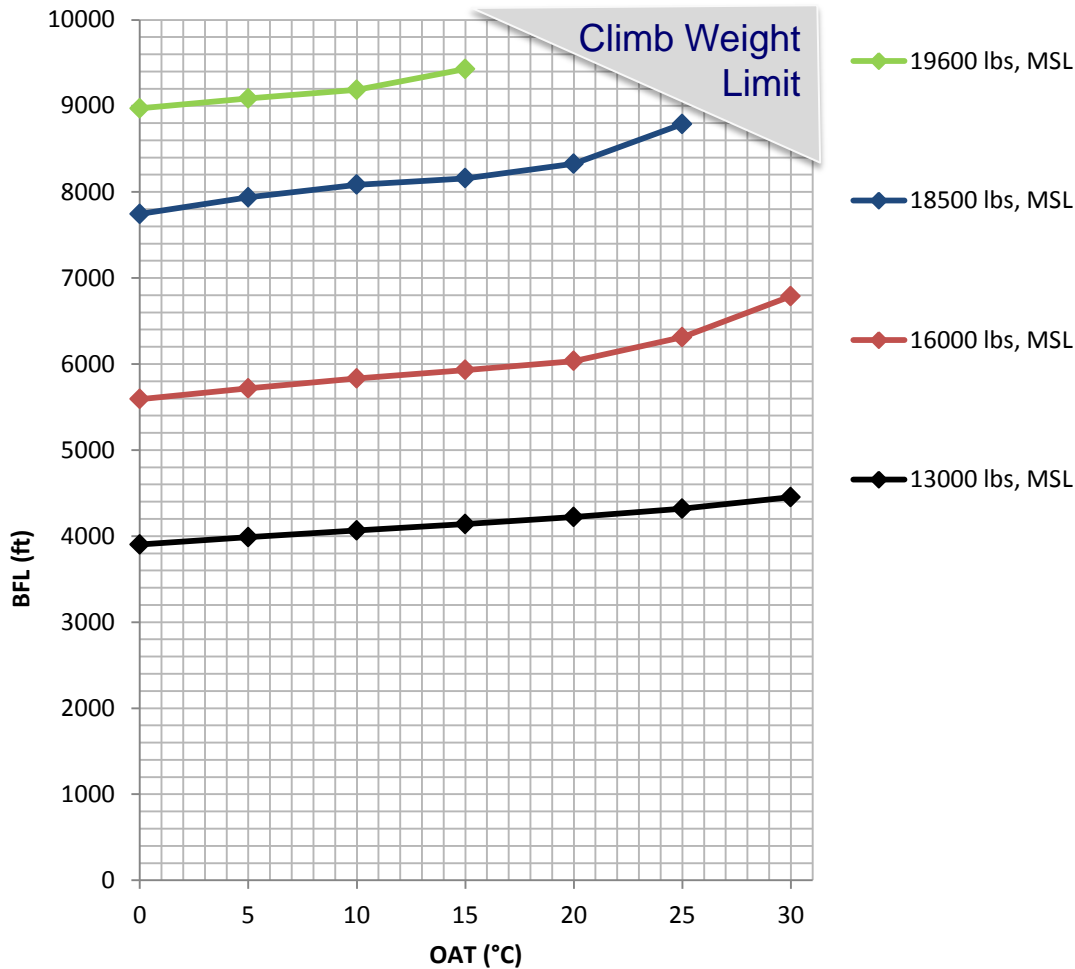
Calculation Approach

Parameters and Forces

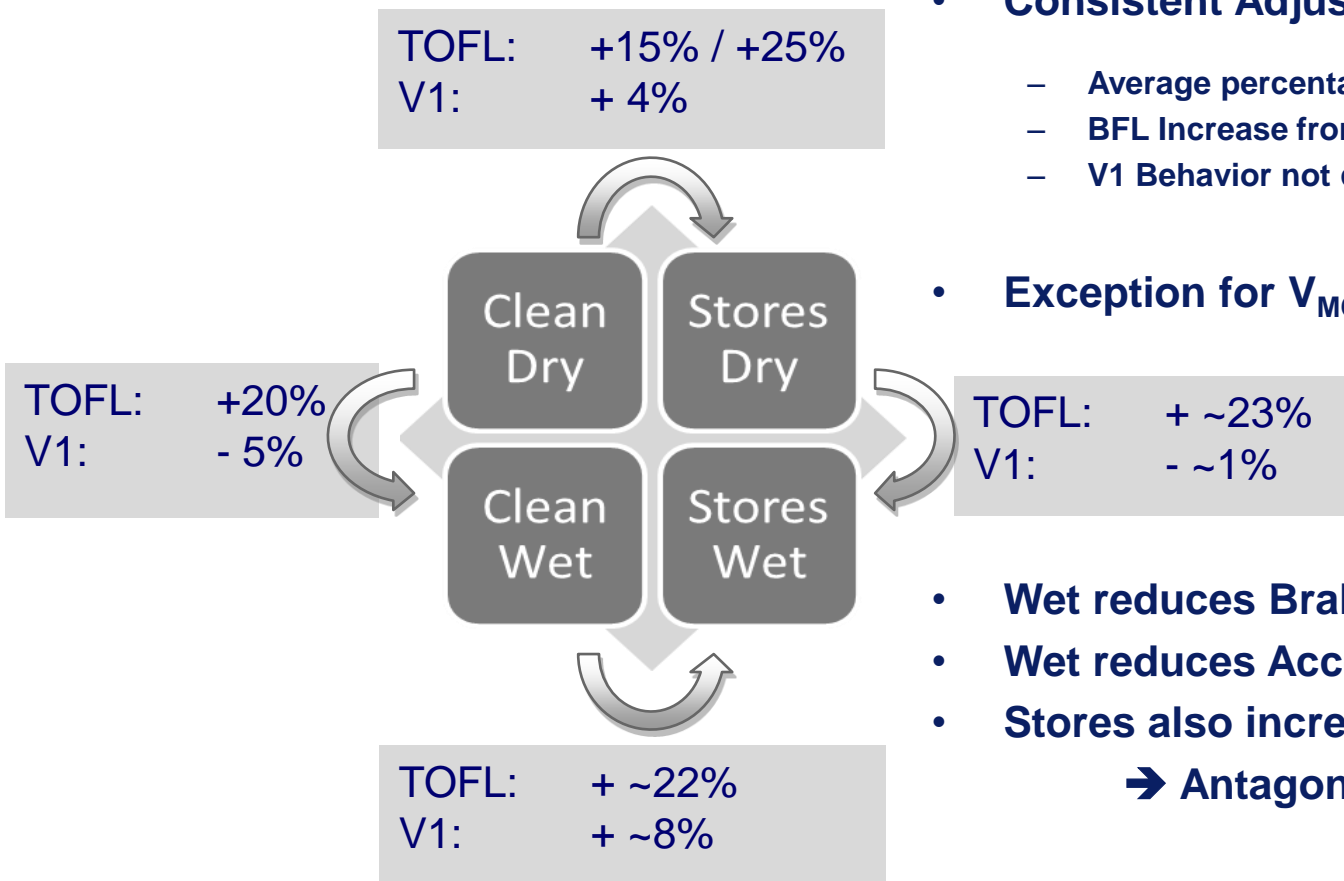
Simulation Results

Conclusions

Simulation Results, MSL



Integration into Four-Corner Sheet

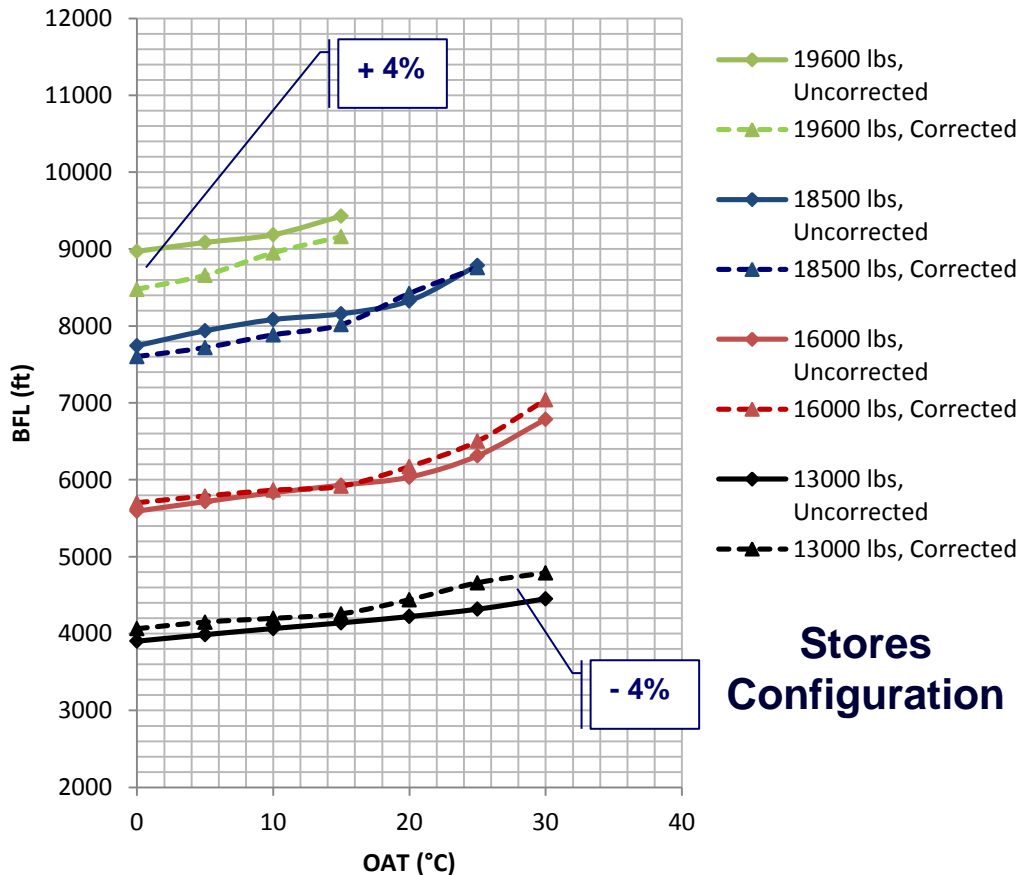


Exception: TOW=13000 lbs

- **Consistent Adjustment Factors**
 - Average percental Values provided for Simulation
 - BFL Increase from all directions, same Magnitudes
 - V1 Behavior not comparable
- **Exception for V_{MCG} - influenced Results**
 - **Wet reduces Braking Performance**
 - **Wet reduces Acceleration Performance**
 - **Stores also increase Braking Performance**
→ Antagonist effect on V_1

Result Deviation to Reference/Calibration

MSL

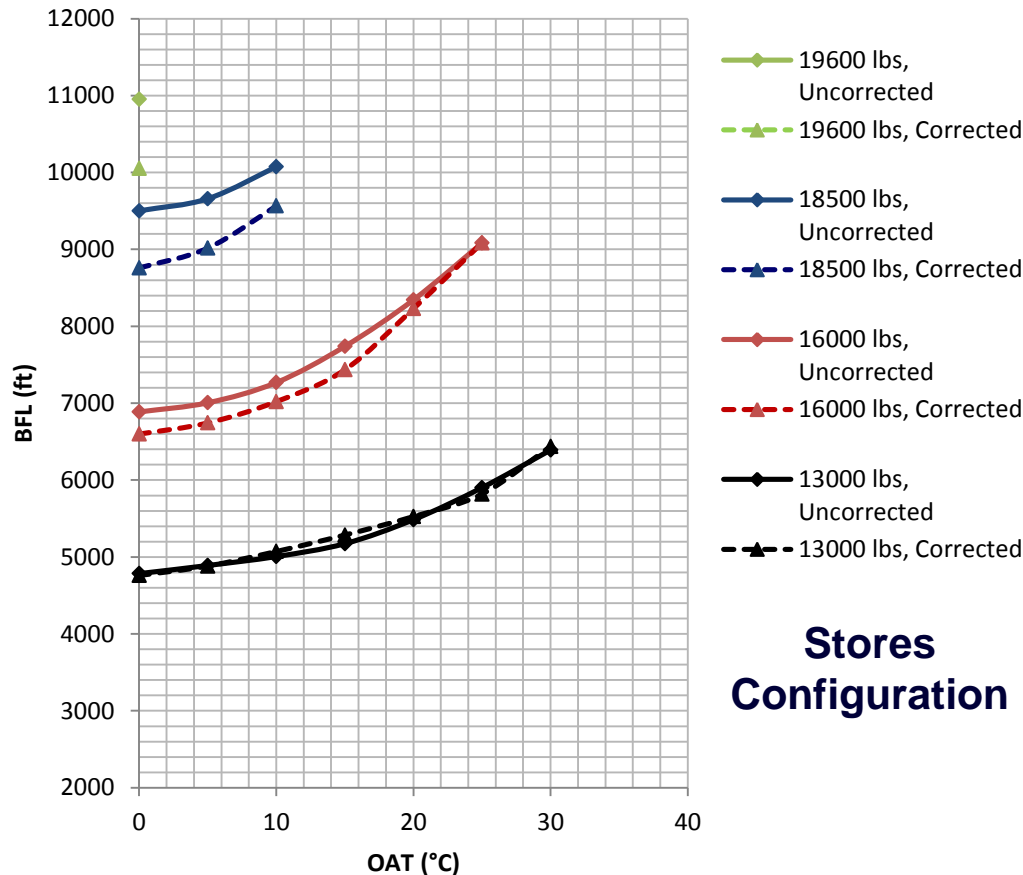


Stores Configuration

- Deviation from Reference Data
 - Small Deviation from AFMS
 - Precision of Simulation comp. to AFMS: average +/- 4% for BFL
 - Simulation conservative for higher TOW
lower OAT
higher PA
 - Calibrated V_1 speeds + 1 KIAS

Result Deviation to Reference/Calibration

4000 ft PA



Stores Configuration

- **Deviation from Reference Data**
 - **Small Deviation from AFMS**
 - **Precision of Simulation comp. to AFMS: average +/- 4% for BFL**
 - **Simulation conservative for higher TOW lower OAT higher PA**
 - **Calibrated V_1 speeds + 1 KIAS**

Parameter Variation Effects

- Testing Variation of Important Parameters to check Plausibility of Results

- Important Parameters:

- Thrust
- Drag
- Rolling and Braking Friction
- V_1 Margin CS-25.109
- Pilot Reaction Time

- Impact of 1 second reaction time considerably high

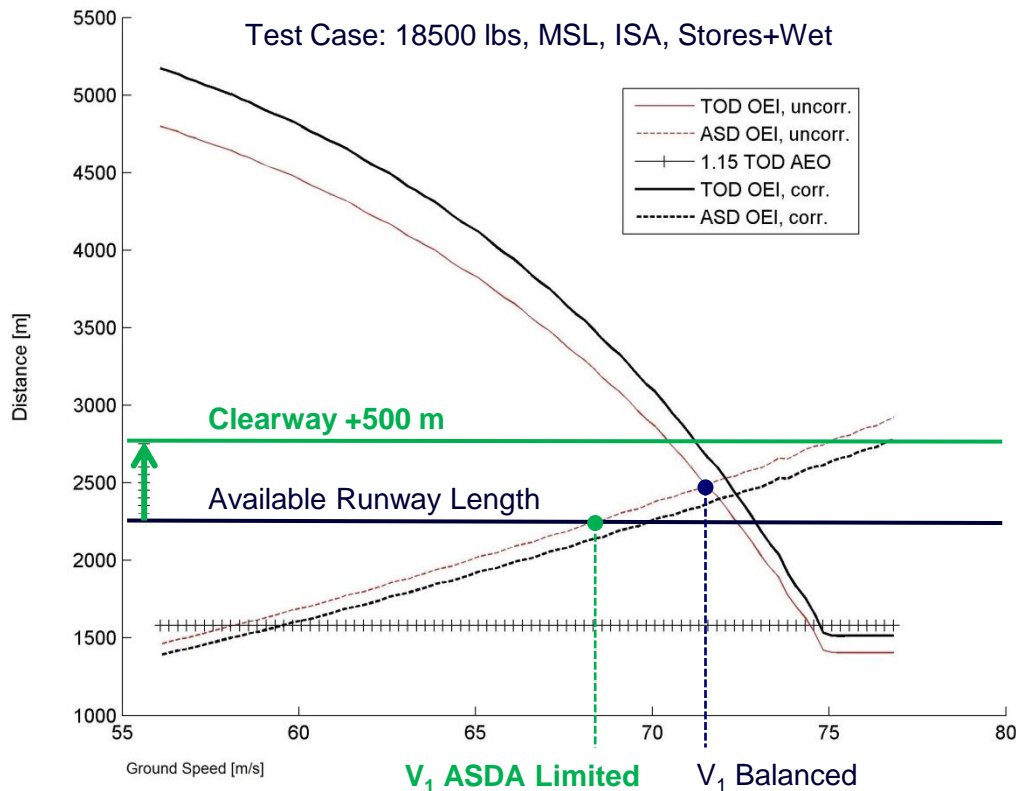
Test Case: 18500 lbs, MSL, ISA

Parameter	Variation	Deviation Impact on BFL,Store
T	10%	-11,83%
T	-10%	15,38%
$C_{D,TO}$	10%	4,65%
$C_{D,TO}$	-10%	-2,90%
$\mu_{roll,wet}$	0,05 static	4,46%
$\mu_{roll,wet}$	10%	2,84%
$\mu_{brake,wet}$	10%	-2,14%
No 2 second margin at V_1	-	-4,02%
React. Time	+1 second	2,38 %

- Aerodynamic Drag high Influence:

Stores Installation creates $\Delta C_D = 0,0136$ (33%) regarding clean aircraft $C_D = 0,0410$

Additional Benefit: BFL - Plots



- Possibility to operate Off-Balance

- Additional Operational Benefit

- Stopway/Clearway may be considered
- TOW may be increased
- TODA/ASDA increase permits takeoff on previously TOW Limited Runways

- Observations from Example

- TODA increased
- Takeoff with Clearway not TOW limited
- ASDA Limited V_1 decreases

Conclusions

- **Validation of Simulation Results**
 - Integration into existing Data coherent
 - Deviations to Reference data relatively small
 - Physical Effects considered in detail and validated
- **Choice of Numerical Simulation Approach**
 - Simulation: High Physical Accuracy
 - Calibration adjusts accuracy to AFMS level (simplified approach, possibly less accurate)
 - Calibration Concept: Beneficial to adjust TOD/ASD Function Parameters
 - Calibration in most cases lower BFL, higher V1 => Simulation Results generally more conservative
- **Level of Detail of Model Data could have been simplified for**
 - Lift Coefficient
 - Spray Impingement Drag
 - Water Skin Friction Drag



Introduction

Calculation
Approach

Parameters
and Forces

Simulation
Results

Conclusions

Additional Benefits of Numerical Simulation

- **High Precision Approach close to physical Reality**
- **Validation of GFD-Adjustment Factor of 1,35 for TOW < 15000 lbs, Clean+Wet**
- **Testing of further aircraft configurations, reaction times, environmental conditions**
- **BFL-Plots with possibility to operate Off-Balance**

Résumé of Important Conclusions

- **Drag effect of Stores almost entirely Aerodynamic also on Wet Runway**
- **Wet Runway + Stores Influence always negative on BFL**
- **V_1 cannot be lowered globally for wet runway conditions**
- **Numerical Takeoff Simulation yields considerable Benefits but:**
 - Detailed Parameter Estimation necessary
 - Precision only possible through constant comparison with AFMS (Calibration)



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Thank You for Your Attention

Balanced Field Length Calculation for a Learjet 35A/36A



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Hamburg University of Applied Sciences

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Image Sources:

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