

AIRCRAFT DESIGN AND SYSTEMS GROUP (AERO)

Induced Drag Estimation of Box Wings for Conceptual Aircraft Design

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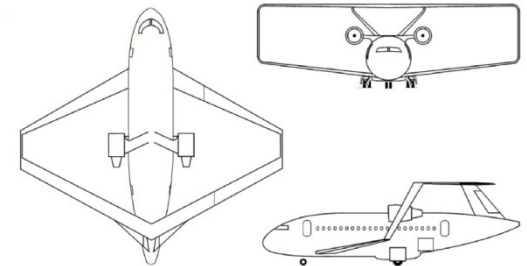
<https://doi.org/10.5281/zenodo.4072303>

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German Aerospace Congress 2019

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Induced Drag Estimation of Box Wings for Conceptual Aircraft Design

Contents

- **Introduction**
- **Induced Drag Calculation from Geometry**
- **Wind Tunnel Measurements**
- **Vortex Lattice Method (VLM) and Comparison with Measurements**
- **Induced Drag with Unequal Lift Share**
- **Summary**

Introduction

Induced Drag Estimation of Box Wings for Conceptual Aircraft Design

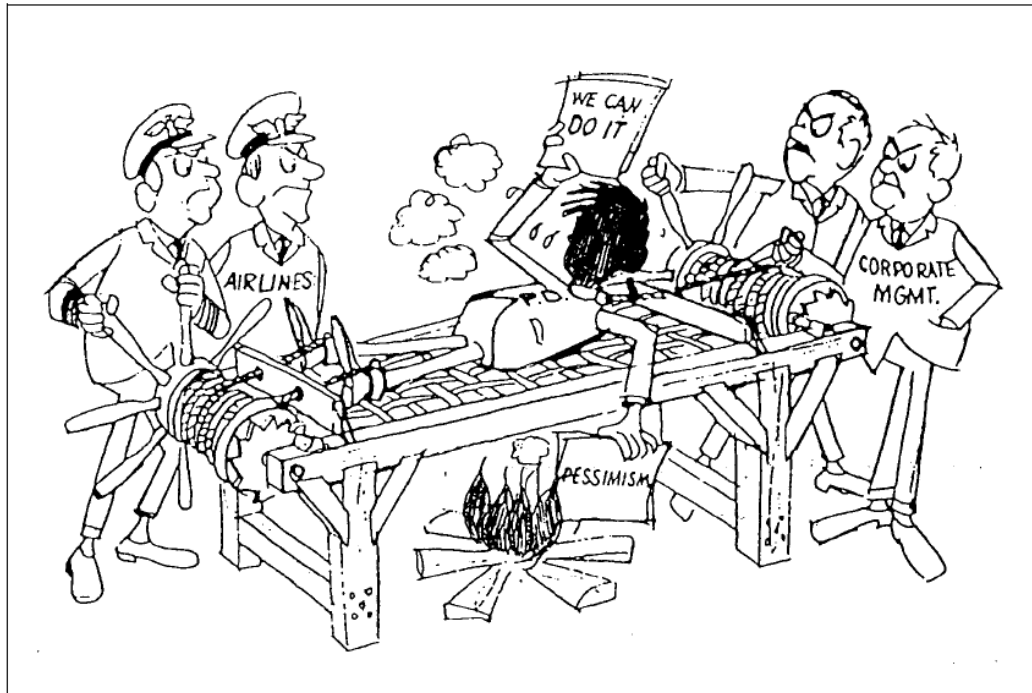


Explanations on the next pages

Introduction

Conceptual Aircraft Design Characteristics

**Early in the project:
Get reliable numbers with simple methods**

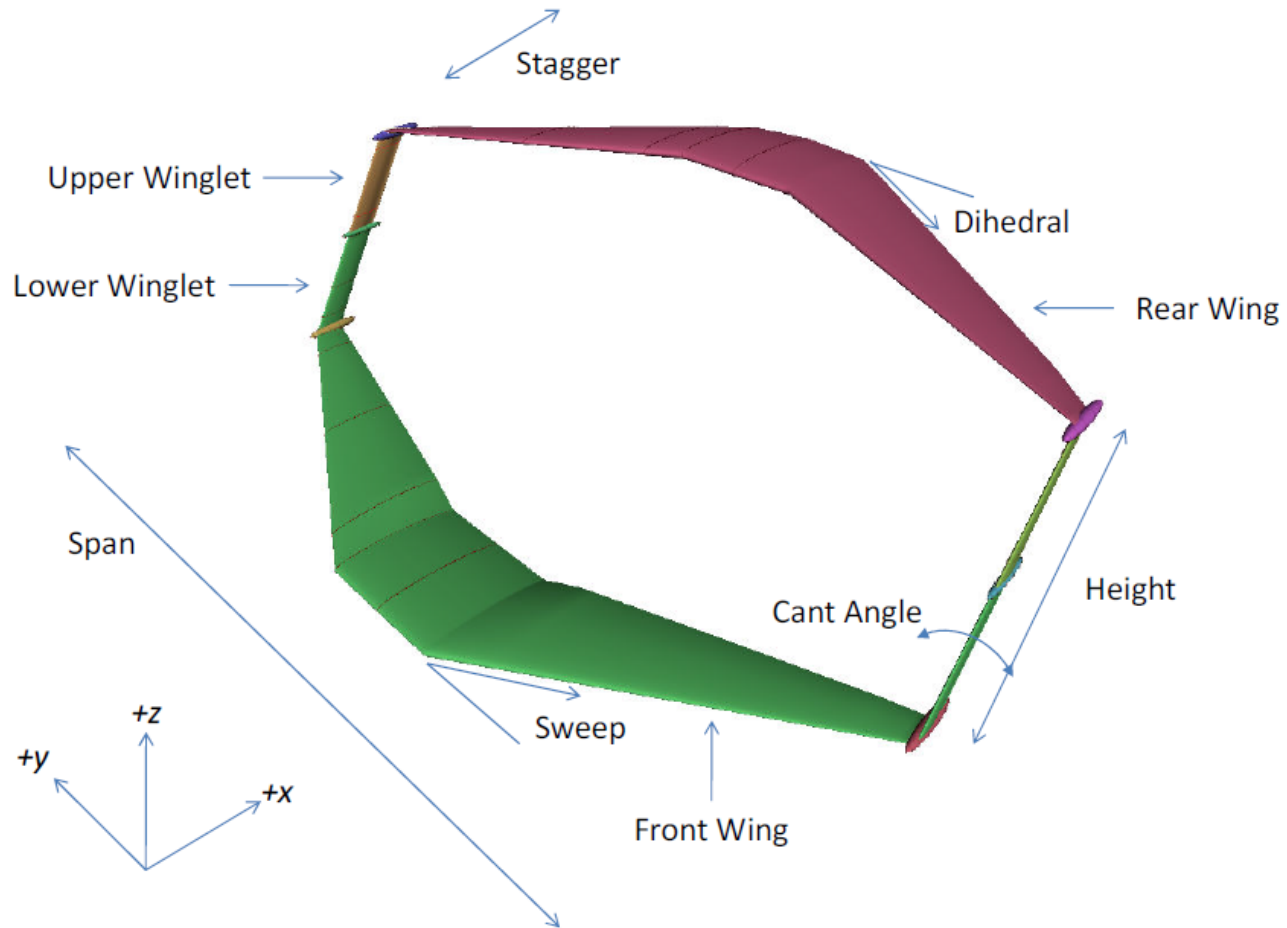


"The design engineer is squeezed by the airlines into final performance guarantees which involve some risk and by his management to avoid that risk"

Scholz 1999

Introduction

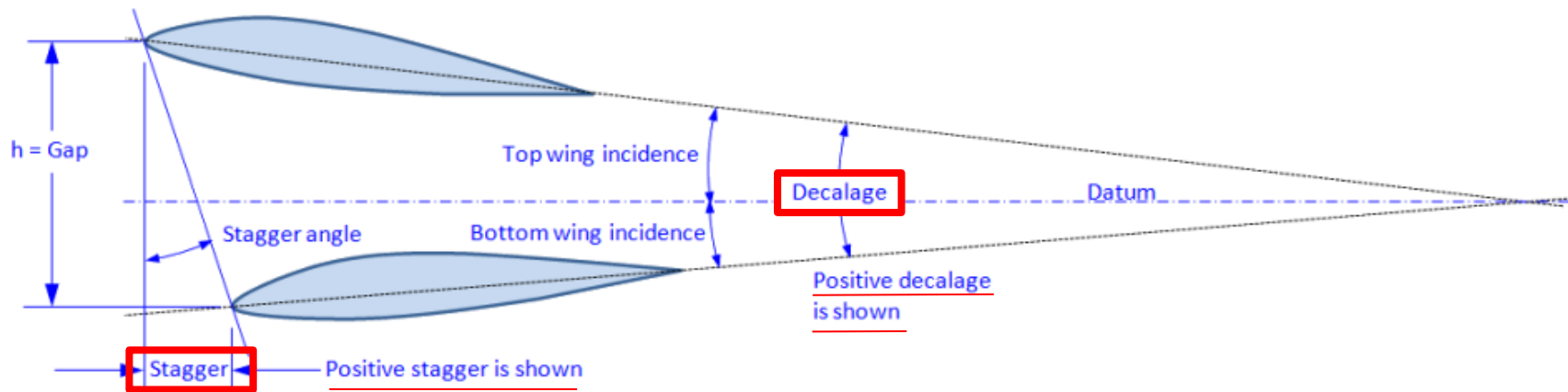
Box Wing



Khan 2010

Introduction

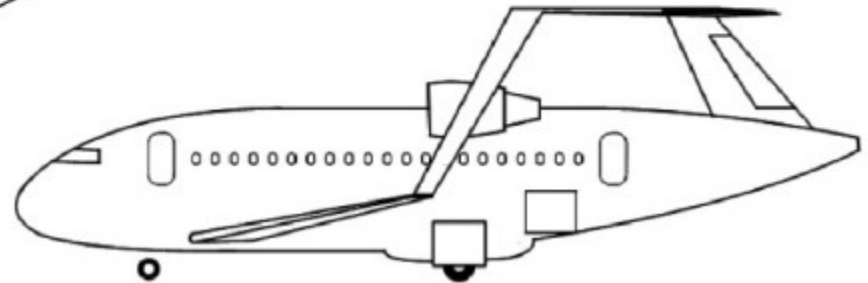
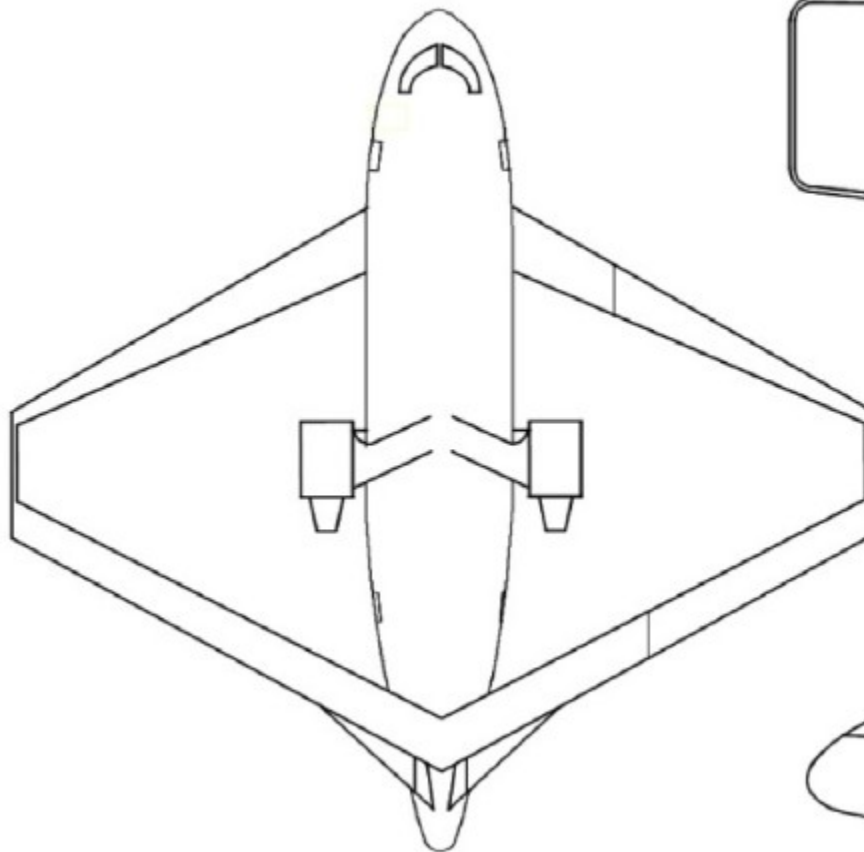
Box Wing



Gudmundsson 2013

Introduction

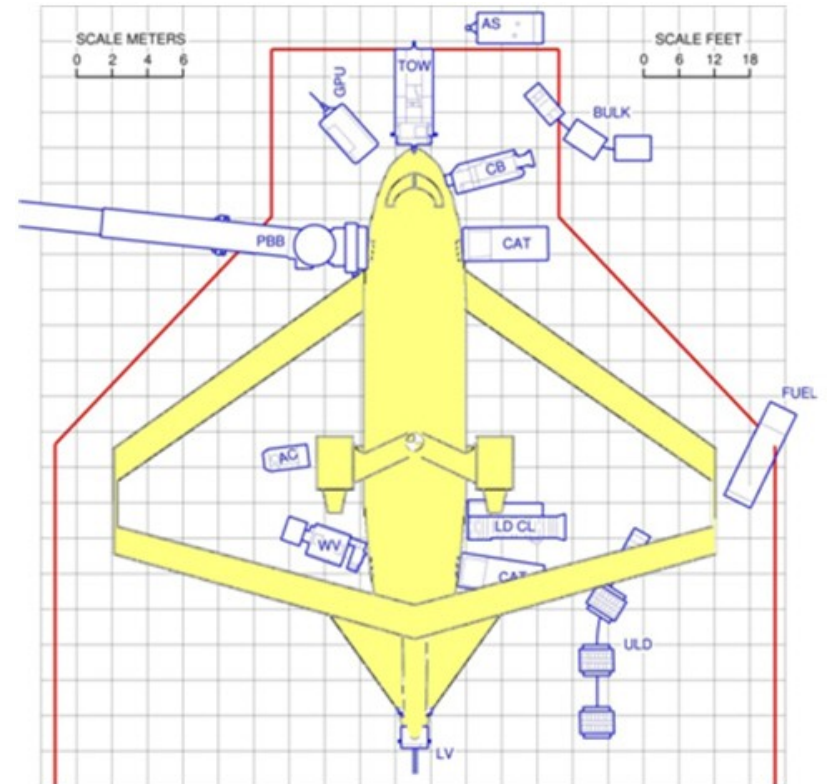
Box Wing Aircraft (BWA) Example



Scholz 2019

Introduction

Box Wing Aircraft (BWA) Example

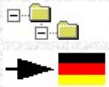


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Introduction

Project "Airport 2030"

<http://Airport2030.ProfScholz.de>



Airport 2030 - Work Task 4.1 Evolutionary Aircraft Configurations Possible A320 Successor



The project "Airport 2030" developed economic concepts and solutions for future air traffic demands. Hamburg University of Applied Sciences (HAW Hamburg) is working on efficient evolutionary aircraft configurations.



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Introduction

Project "Airport 2030" with Designs of Two **Box Wing Aircraft**



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Introduction

Video: **Box Wing Aircraft** in Flight



Model Editor: "Plane Maker"

Simulator: "X-Plane"

Aircraft flown by hand

Video

<https://youtu.be/en65adjJpgk>

on

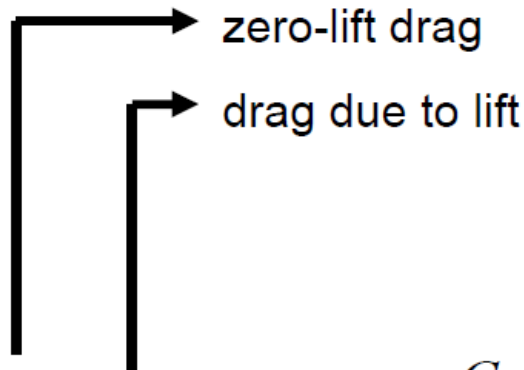
<http://youtube.ProfScholz.de>

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Introduction

Induced Drag / Drag due to Lift

Airplane drag



$$C_D = C_{D,0} + C_{D,i} = C_{D,0} + \frac{C_L^2}{\pi A e} = C_{D,0} + \frac{C_L^2}{\pi A} (1 + \delta)$$

↑
Oswald factor e

Induced Drag Calculation from Geometry

Induced Drag Calculation from Geometry

Calculate Oswald Factor e Without Input of C_{D0}

$$e = e_{theo} \cdot k_{e,F} \cdot k_{e,D_0} \cdot k_{e,M}$$

e

Oswald factor:

correction factor for the aspect ratio to calculate drag due to lift

e_{theo}

theoretical Oswald factor, inviscid drag due to lift only

$k_{e,F}$

correction factor: losses due to the fuselage

k_{e,D_0}

correction factor: viscous drag due to lift

$k_{e,M}$

correction factor: compressibility effects on induced drag

Nita 2012

Induced Drag Calculation from Geometry

Calculating parameters $k_{e,F}$, $k_{e,D0}$, $k_{e,M}$

$$e = e_{theo} \cdot k_{e,F} \cdot k_{e,D0} \cdot k_{e,M}$$

e_{theo} see next pages

$$k_{e,F} = 1 - 2 \left(\frac{d_F}{b} \right)^2$$

$$k_{e,M} = a_e \left(\frac{M}{M_{comp}} - 1 \right)^{b_e} + c_e$$

$$a_e < 0; \quad c_e = 1$$

$$a_e = -0.00152$$

$$b_e = 10.82$$

$$c_e = 1$$

$$M_{comp} = 0.3$$

Aircraft category	d_F / b	$k_{e,F}$	$k_{e,D0}$
All	0.114	0.974	-
Jet	0.116	0.973	0.873
Business Jet	0.120	0.971	0.864
Turboprop	0.102	0.979	0.804
General Aviation	0.119	0.971	0.804

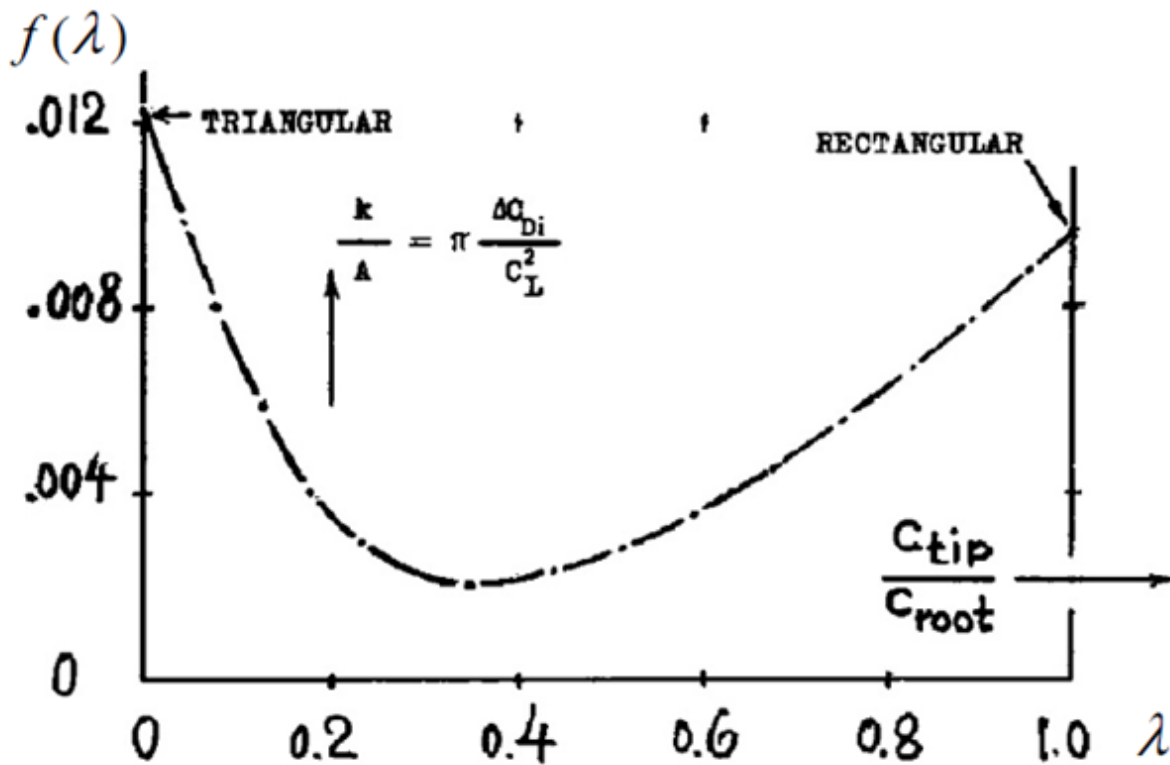
Parameters a_e and b_e are for cruise Mach number, M_{CR} around 0.8. For significant other M_{CR} see Scholz 2012.

Nita 2012

Induced Drag Calculation from Geometry

Calculating Parameter e_{theo}

Corrections to induced drag for **unswept*** wings as a function of taper ratio λ



$$f(\lambda) = k / A$$

$$C_{Di} = (1 + k) C_L^2 / \pi A$$

$$k = \delta$$

$$e_{theo} = \frac{1}{1 + \delta}$$

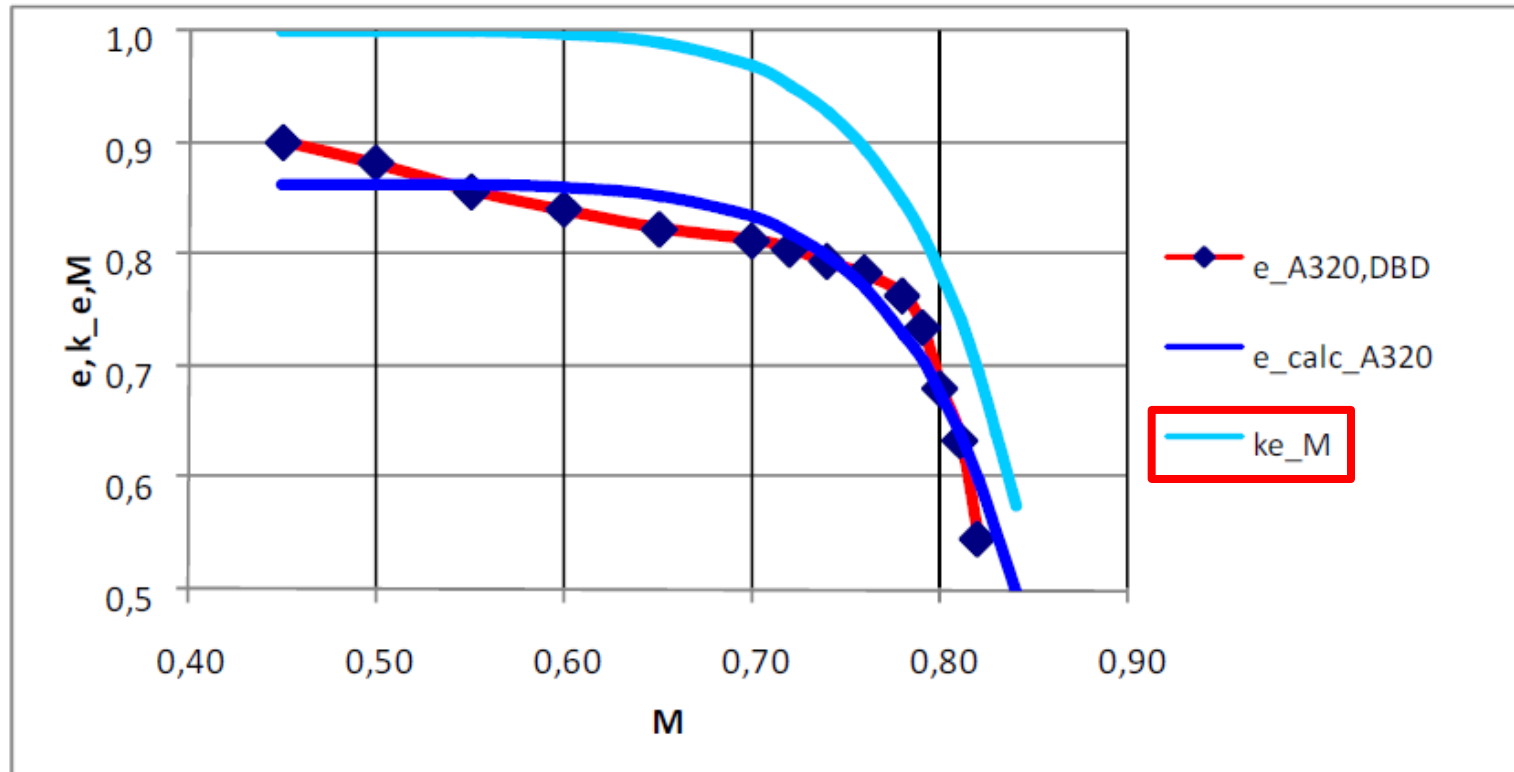
$$e_{theo} = \frac{1}{1 + f(\lambda) \cdot A}$$

* For swept wings see Nita 2012

Nita 2012

Induced Drag Calculation from Geometry

Influence of Mach Number Tuned to A320 Data: $k_{e,M}$

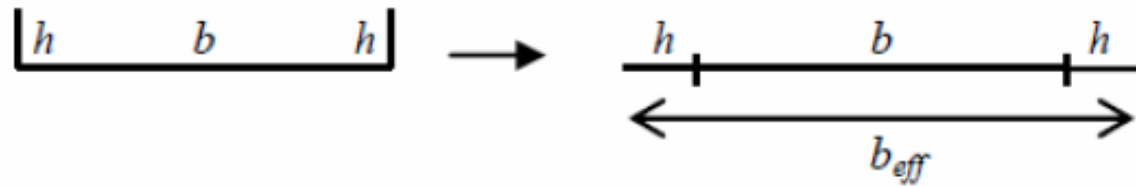


$k_{e,M}$ is calculated here with $a_e = -0,00270$ and $b_e = 8,60$ optimized for the A320.

Nita 2012

Induced Drag Calculation from Geometry

Estimating the Span Efficiency Factor for Non-Planar Configurations



The following relations can be derived from geometry:

$$\frac{b_{eff}}{b} = 1 + 2 \frac{h}{b}$$

$$C_{D,i} = \frac{C_L^2}{\pi A e}$$

$$C_{D,i,WL} = \frac{C_L^2}{\pi A_{eff} e} = \frac{C_L^2}{\pi A e_{WL}}$$

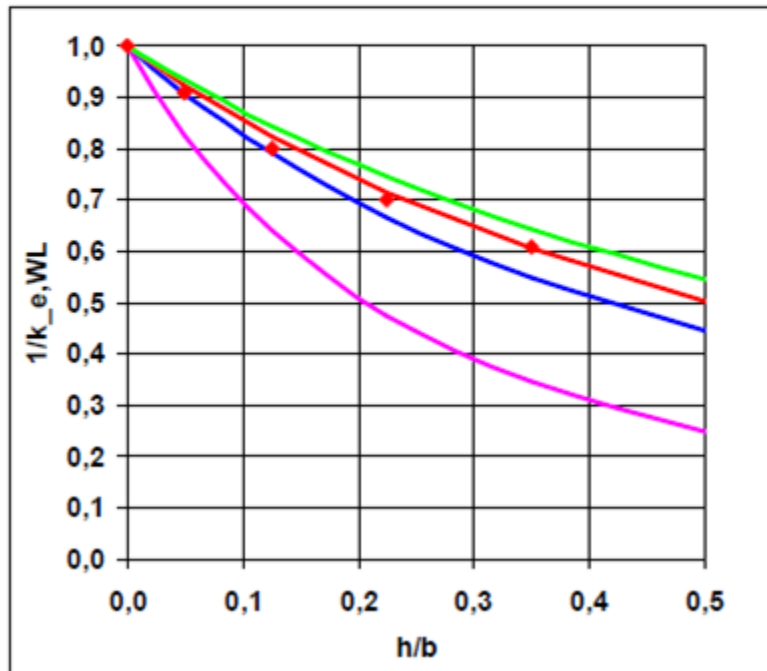
$$e_{WL} = \frac{A_{eff}}{A} \cdot e = \left(\frac{b_{eff}}{b} \right)^2 \cdot e \quad \rightarrow \quad e_{WL} = \left(1 + 2 \frac{h}{b} \right)^2 \cdot e$$

Nita 2012

Induced Drag Calculation from Geometry

Correction of the Simple Geometrical Consideration via the Factor k_{WL}

$$e_{WL} = \left(1 + \frac{2}{k_{WL}} \frac{h}{b}\right)^2 \cdot e = k_{e,WL} \cdot e = e_{theo} \cdot k_{e,F} \cdot k_{e,D_0} \cdot k_{e,M} \cdot k_{e,WL}$$



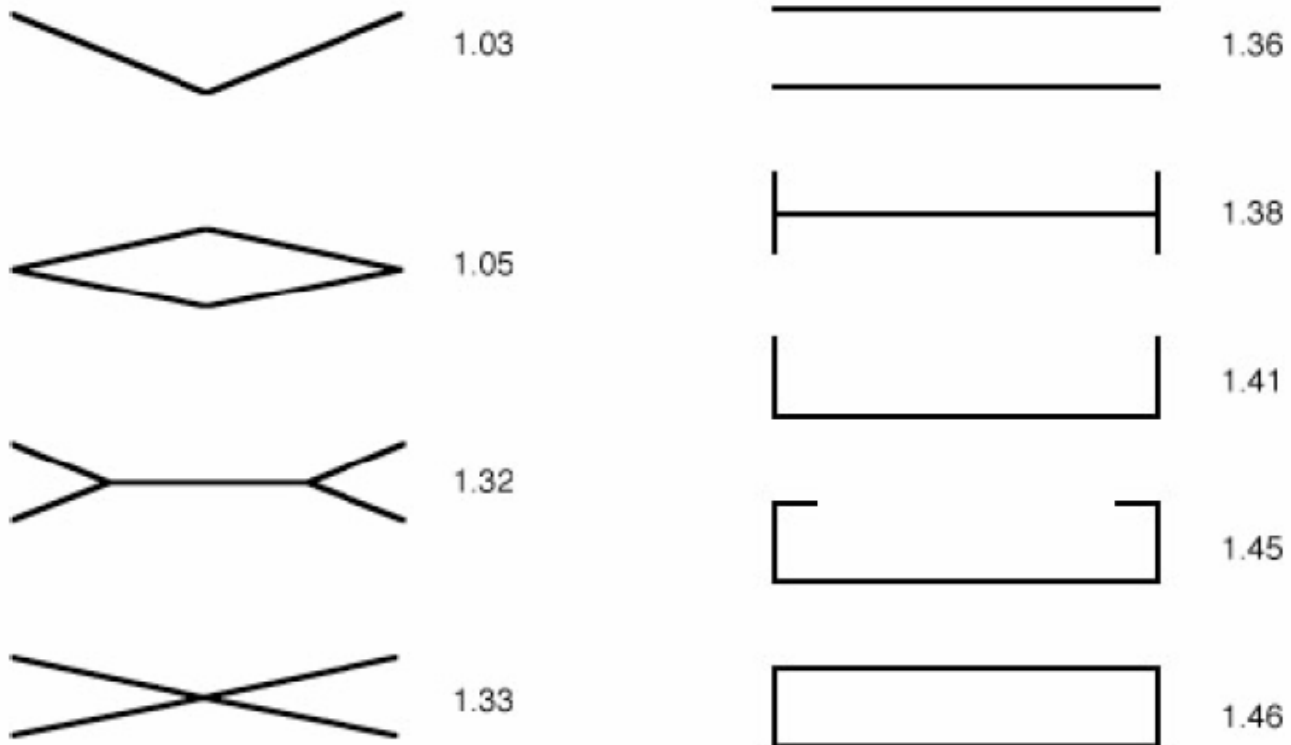
$$k_{e,WL} = \left(1 + \frac{2}{k_{WL}} \frac{h}{b}\right)^2 = \frac{A_{eff}}{A} = \left(\frac{b_{eff}}{b}\right)^2$$

- ◆ DUBS, read from diagram
- geometry, $k_{wl} = 1$
- HOWE, $k_{wl} = 2$
- DUBS, ZIMMER, $k_{wl} = 2.45$
- real A/C average, $k_{wl} = 2.83$

Nita 2012

Induced Drag Calculation from Geometry

Relative Span Efficiency Factors e_{NP}/e for Wing Configurations Beyond Winglets



Span efficiency for various optimally loaded non-planar systems ($h/b = 0.2$)

Kroo 2005

Induced Drag Calculation from Geometry

Generalization of the Winglet Equation for Nonplanar Wings: $k_{WL} \Rightarrow k_{NP}$

The following relations can be written: (this time via a penalty factor called k_{NP})

$$e_{NP} = \left(1 + \frac{2}{k_{NP}} \frac{h}{b} \right)^2 \cdot e \Leftrightarrow e_{NP} = k_{e,NP} \cdot e$$

The factor for wings with winglets and dihedral, investigated above, becomes now a particular case of the factor k_{NP} .

Having the $k_{e,NP}$ from KROO, k_{NP} can be calculated for each configuration

$$k_{NP} = 2 \frac{h}{b} \cdot \frac{1}{\sqrt{k_{e,NP} - 1}}$$

Numbers on next page!







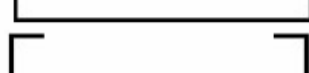
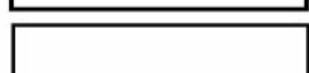

Induced Drag Calculation from Geometry

Generalization of the Winglet Equation: Numbers for k_{NP}

$$e_{NP} = \left(1 + \frac{2}{k_{NP}} \frac{h}{b} \right)^2 \cdot e = k_{e,NP} \cdot e$$

$$= e_{theo} \cdot k_{e,F} \cdot k_{e,D_0} \cdot k_{e,M} \cdot k_{e,NP}$$



	$h/b = 0.2$	general
Non-planar configuration	$k_{e,NP}$	k_{NP}
	1.03	26.9
	1.05	16.2
	1.32	2.69
	1.33	2.61
	1.36	2.41
	1.38	2.29
	1.41	2.13
	1.45	1.96
	1.46	1.92

Nita 2012

Induced Drag Calculation from Geometry

An Equation with Another Structure for the Box Wing

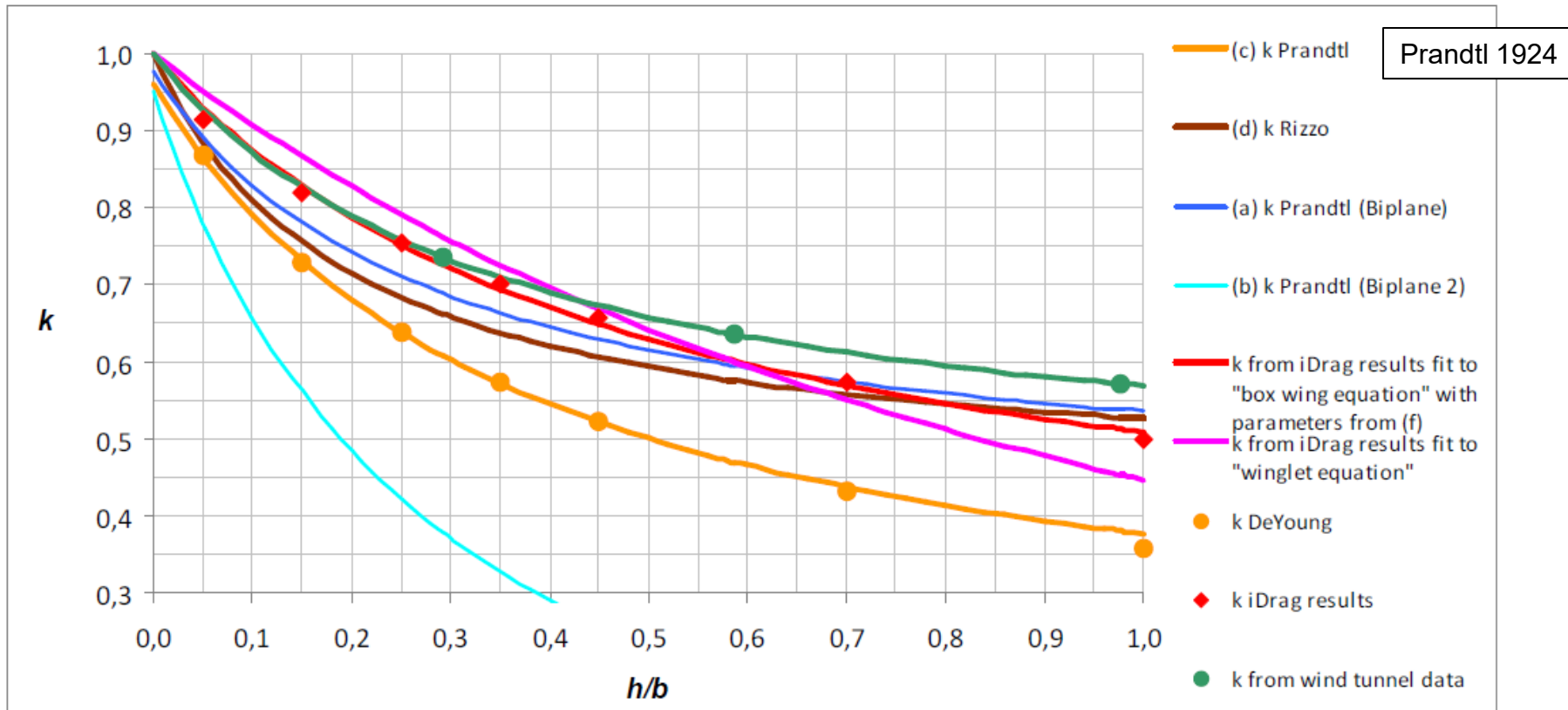
$$\frac{e_{NP}}{e} = k_{e,NP} = 1/k$$

$$\frac{D_{i,box}}{D_{i,ref}} = k = \frac{k_1 + k_2 \cdot h/b}{k_3 + k_4 \cdot h/b}$$

box wing equation

Induced Drag Calculation from Geometry

Initial Data Comparison from DLRK 2012 (Nita 2012)



DLRK 2012:

Proceedings:

Paper:

Deutscher Luft- und Raumfahrtkongress (German Aerospace Congress), Berlin, 2012

<http://www.dlrk2012.dglr.de/publikationen>

<https://nbn-resolving.org/urn:nbn:de:101:1-201212176728>

Induced Drag Calculation from Geometry

Curve Fitting Results from DLRK 2012 (Nita 2012)

Case	Configuration	Author	k_1	k_2	k_3	k_4	k for $h/b \rightarrow 0$	k for $h/b \rightarrow \infty$
(a)	Biplane	Prandtl*	1	-0.66	2.1	7.4	0.976	-0.089
(b)	Biplane (2)	Prandtl	1	-0.66	1.05	3.7	0.952	-0.178
(c)	Box wing	Prandtl	1	0.45	1.04	2.81	0.962	0.160
(d)	Box wing	Rizzo	0.44	0.959	0.44	2.22	1	0.432
(e)	Box wing	iDrag best fit	1.304	0.372	1.353	1.988	0.964	0.187
(f)	Box wing	iDrag $k_1 = k_3$	1.037	0.571	1.037	2.126	1	0.269

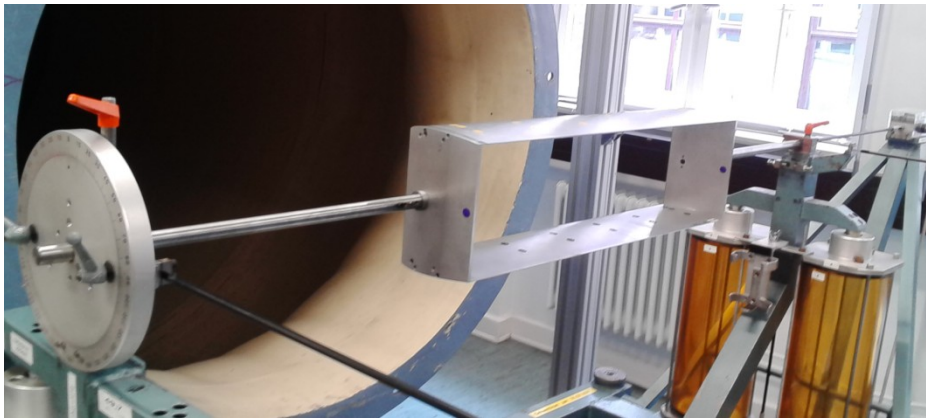
* here, a different equation is used: $k = 0.5 + \frac{k_1 + k_2 \cdot h/b}{k_3 + k_4 \cdot h/b}$

Subsequent additional wind tunnel measurements and calculation with VLM showed room for improvement !

Wind Tunnel Measurements

Wind Tunnel Measurements

Wind Tunnel and Force Measurements

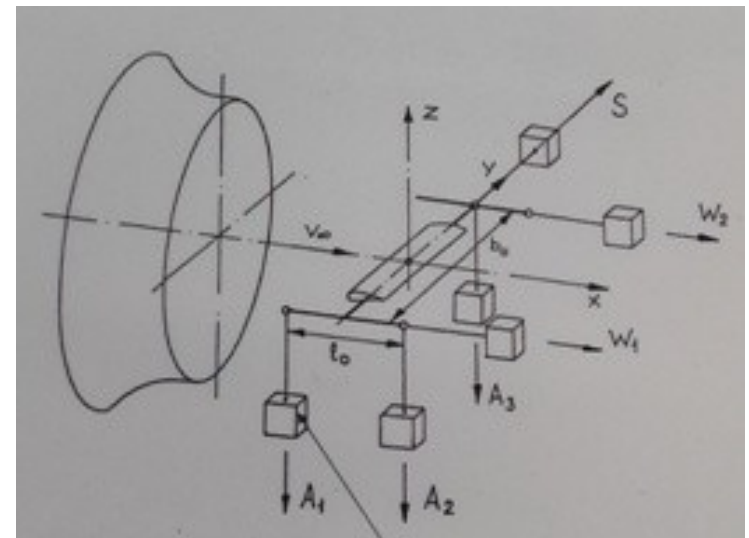
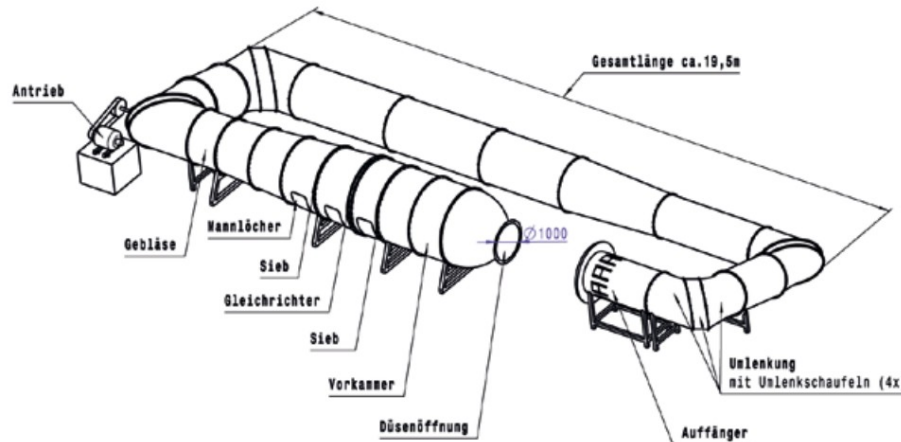


Wind tunnel with open test section
(Göttingen-Type)

Chord, c : 100 mm

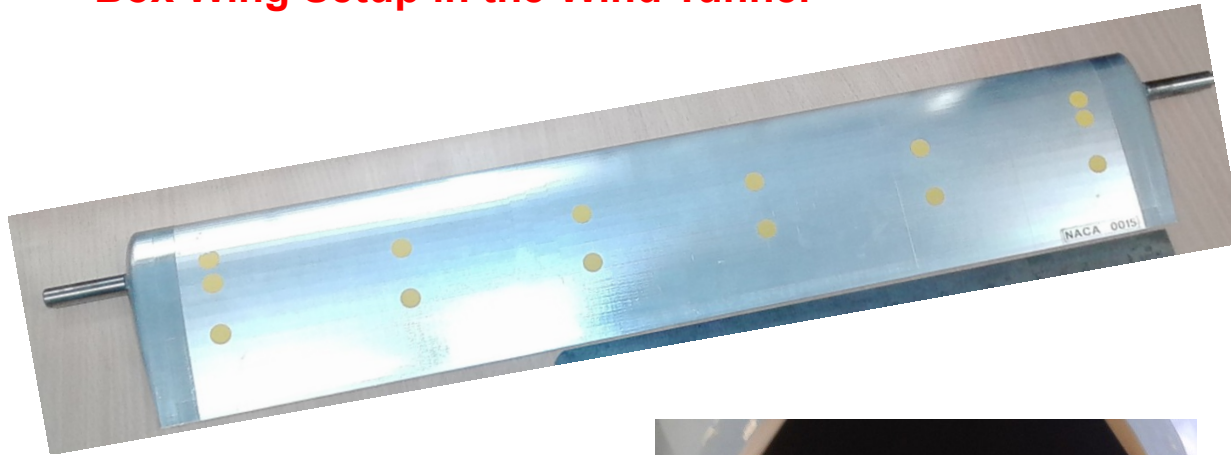
Reynoldsnumber, Re : 160000

Air speed ≈ 25 m/s



Wind Tunnel Measurements

Box Wing Setup in the Wind Tunnel



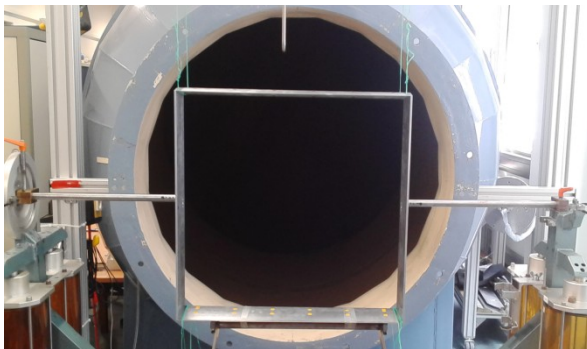
Airfoil used: NACA0015

Reference wing:

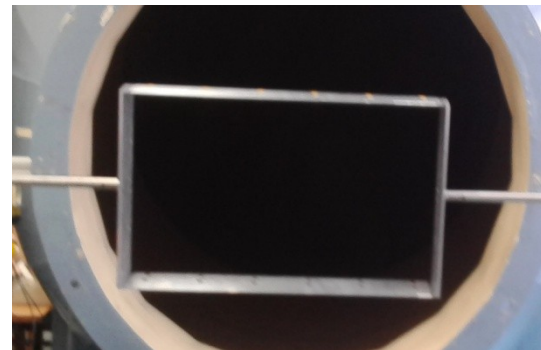
span, b : 520 mm

chord, c : 100 mm

$$A = b/c = b^2 / S = 5.2$$



$$h/b = 0.93$$



$$h/b = 0.62$$



Box wings from
two reference wings:

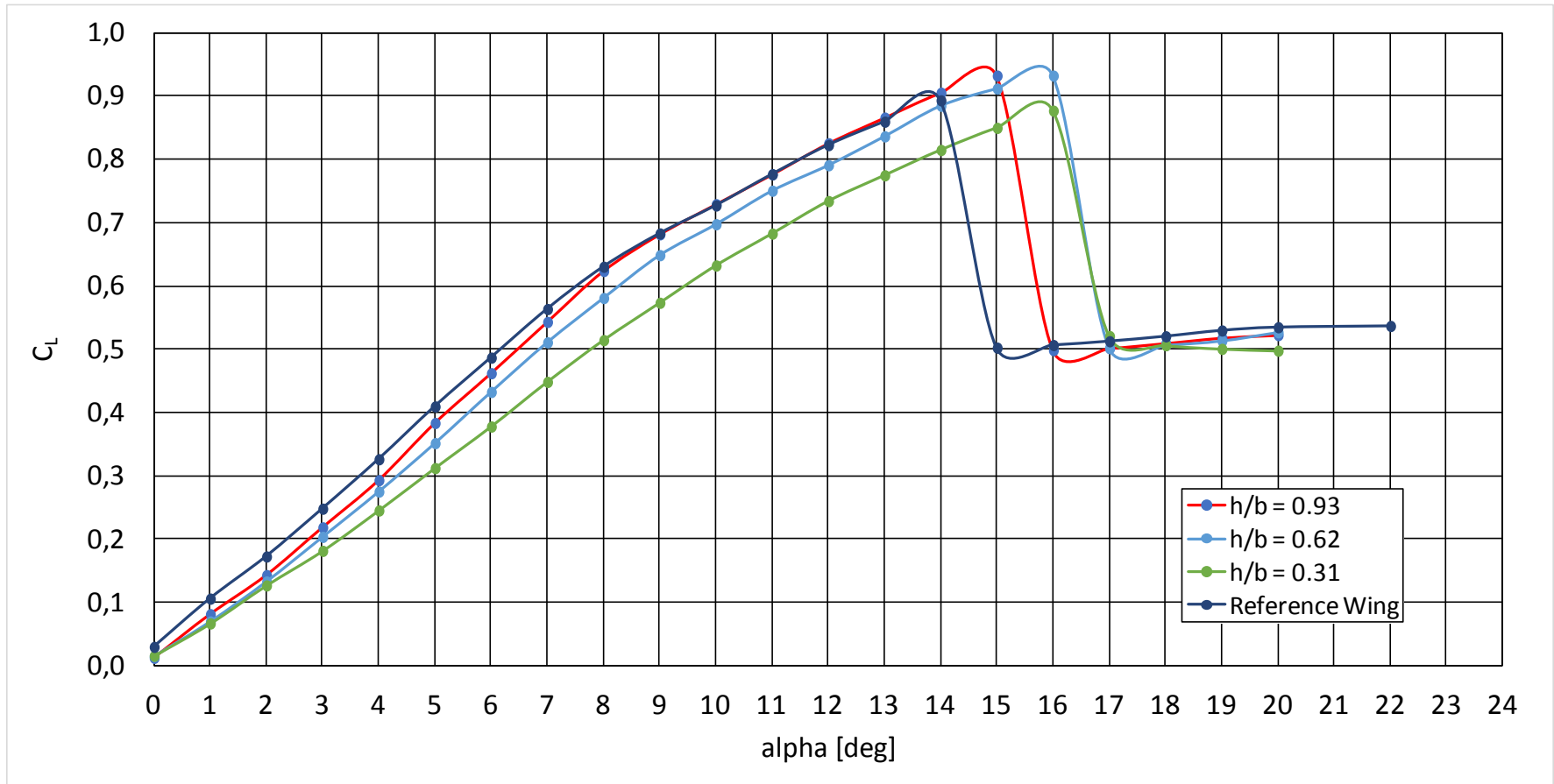
$$A = b^2 / S = 2.6$$

height (h) to span (b) ratio:

$$h/b = 0.31$$

Wind Tunnel Measurements

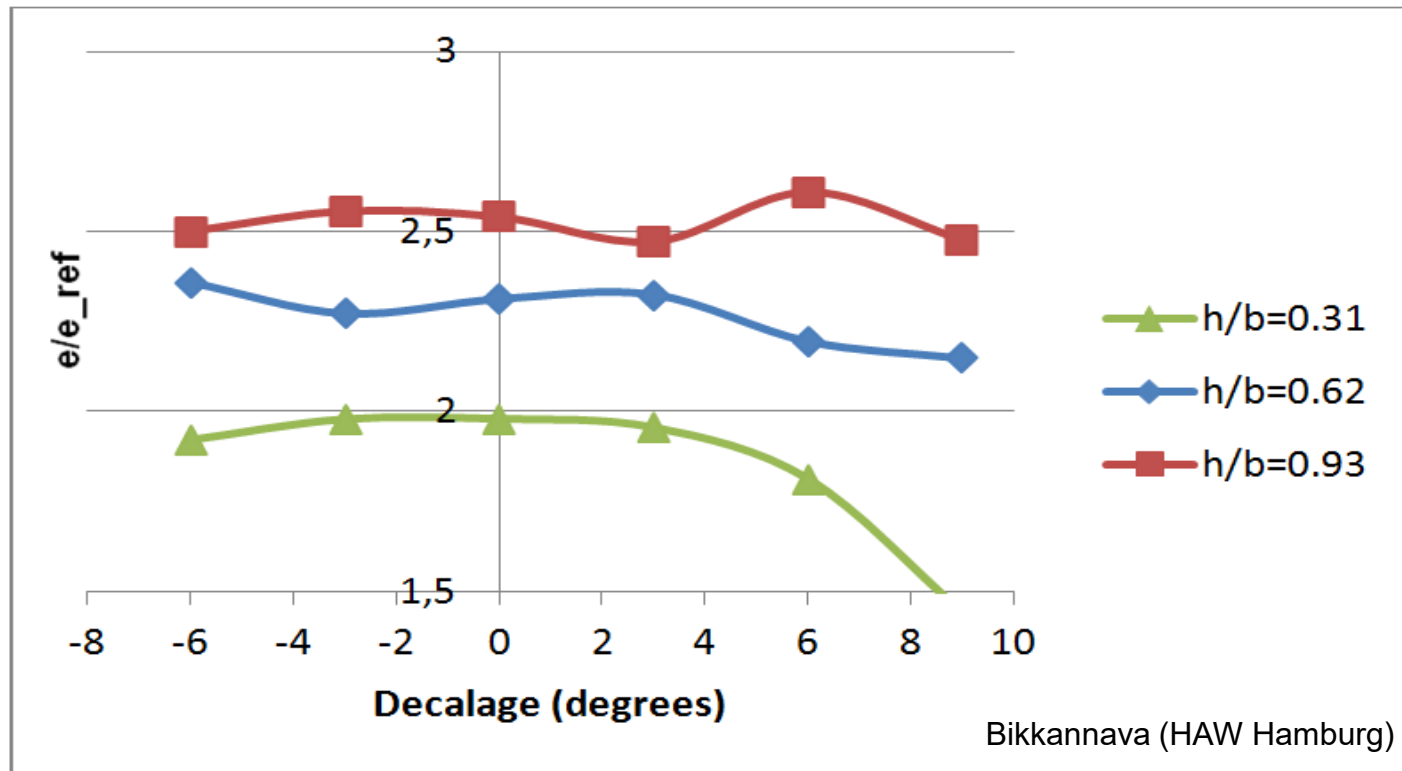
Box Wing $C_L = f(\alpha)$

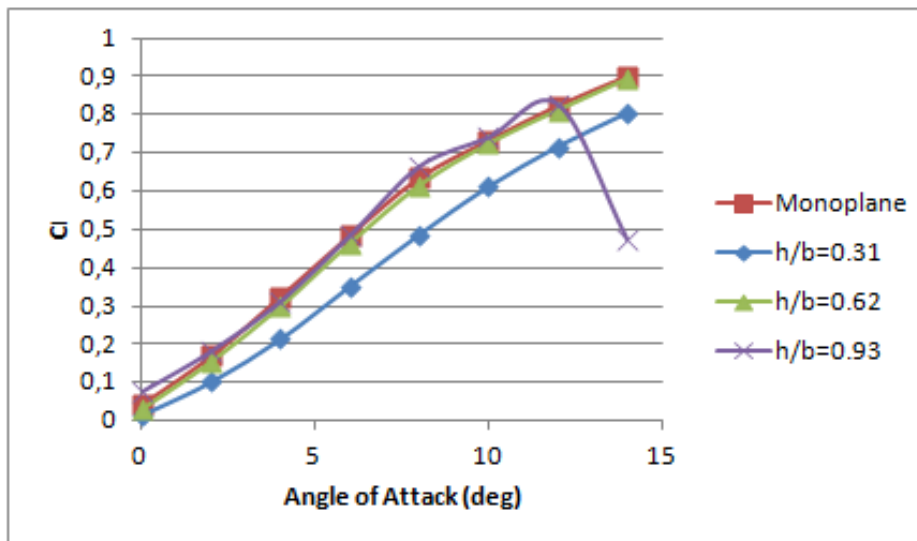


Ribeiro (HAW Hamburg)

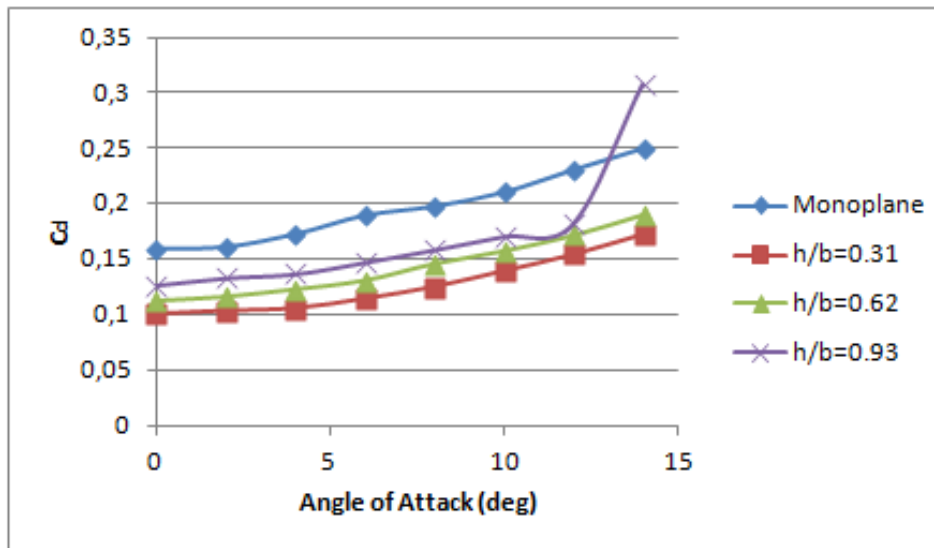
Wind Tunnel Measurements

Decalage: No Systematic Advantage => Advice: Do Not Apply Decalage!





Lift Coefficient v/s AoA, no decalage



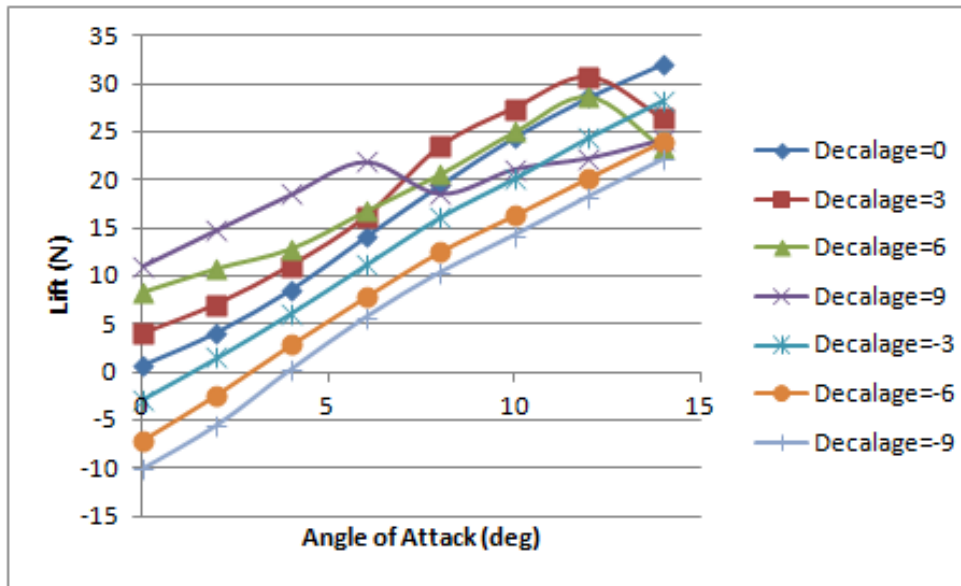
Drag Coefficient v/s AoA, no decalage

all h/b

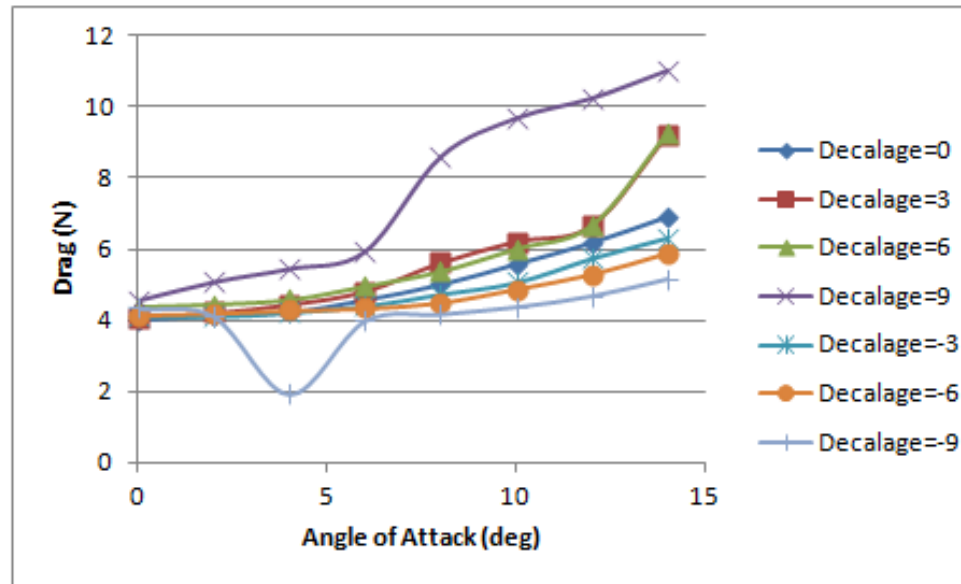
no decalage

Absolute drag coefficient not representative !

Bikkannavar (HAW Hamburg)



$h/b=0.31$ Lift vs. AoA



$h/b=0.31$ Drag vs. AoA

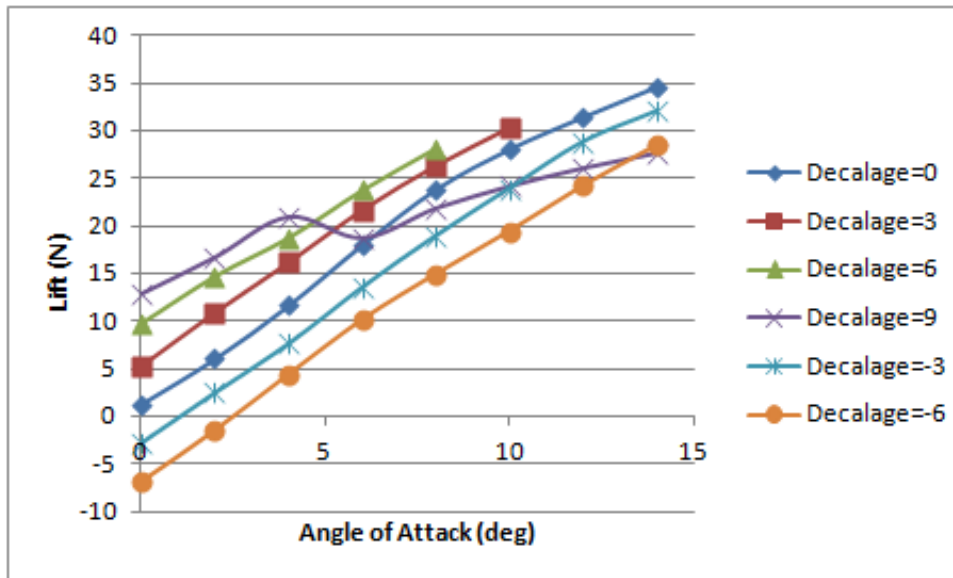
decalage

and

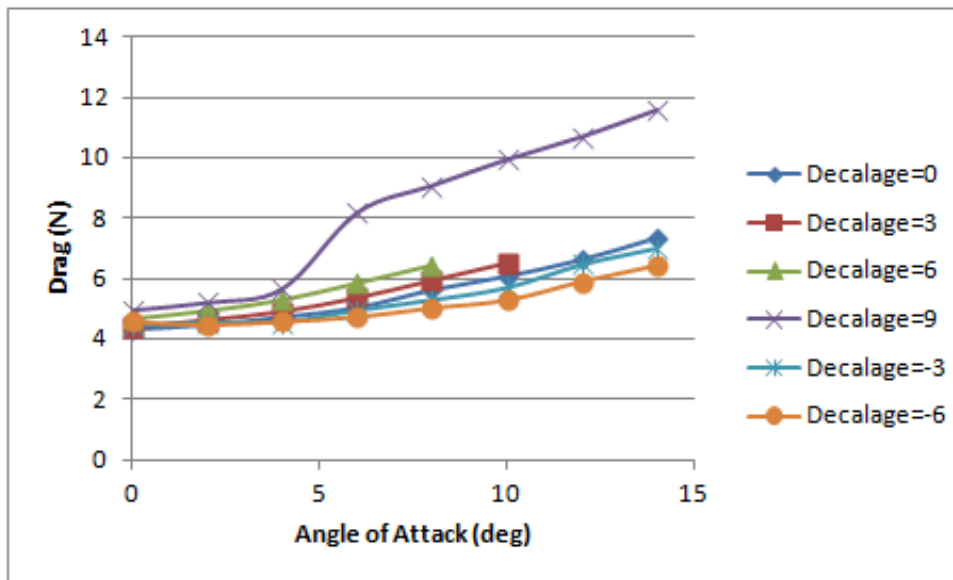
$h/b = 0.31$

Absolute drag not representative !

Bikkannavar (HAW Hamburg)



h/b=0.62 Lift vs. AoA



h/b=0.62 Drag vs. AoA

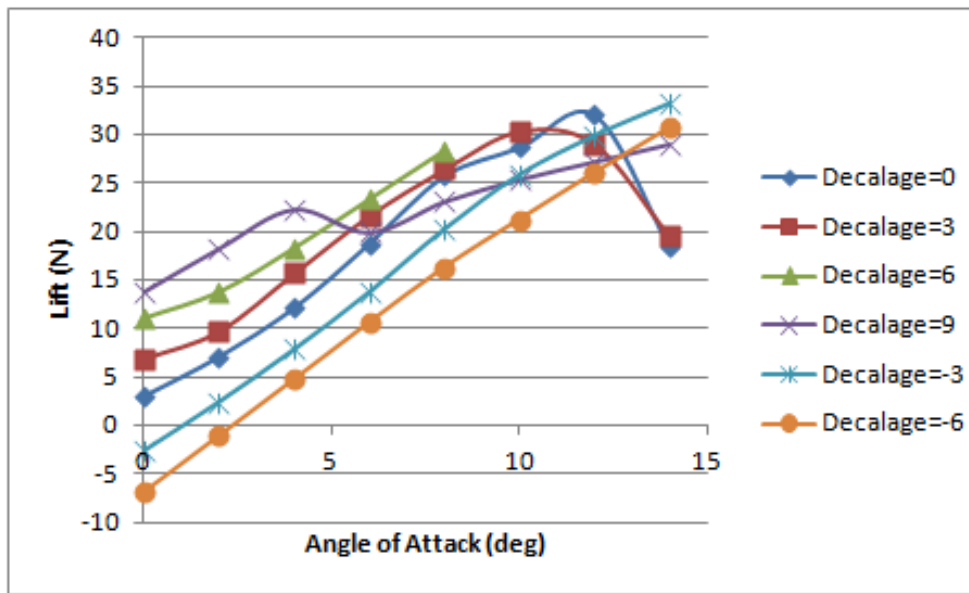
decalage

and

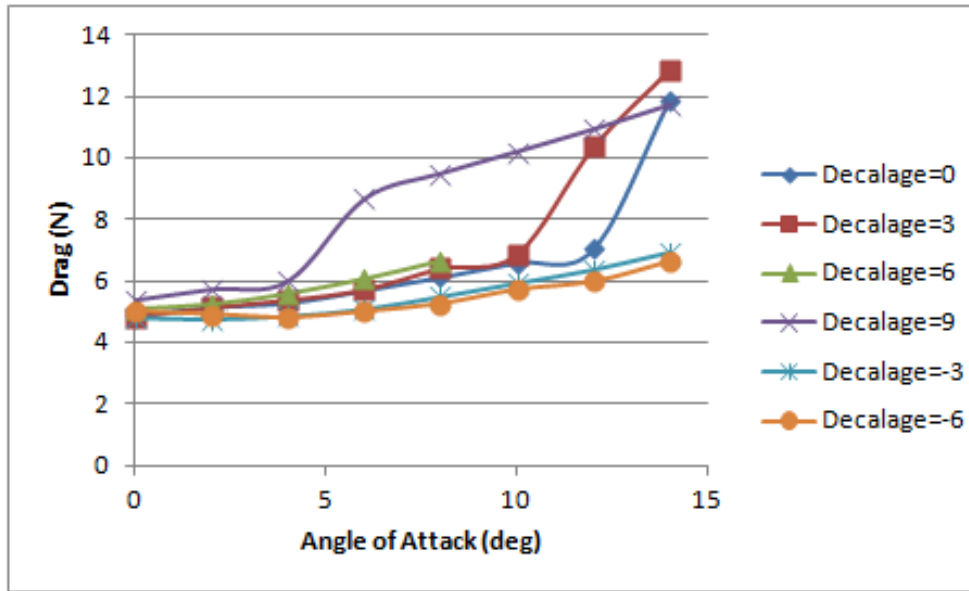
h/b = 0.62

Absolute drag not representative !

Bikkannavar (HAW Hamburg)



h/b=0.93 Lift vs. AoA



h/b=0.93 Drag vs. AoA

decalage

and

h/b = 0.93

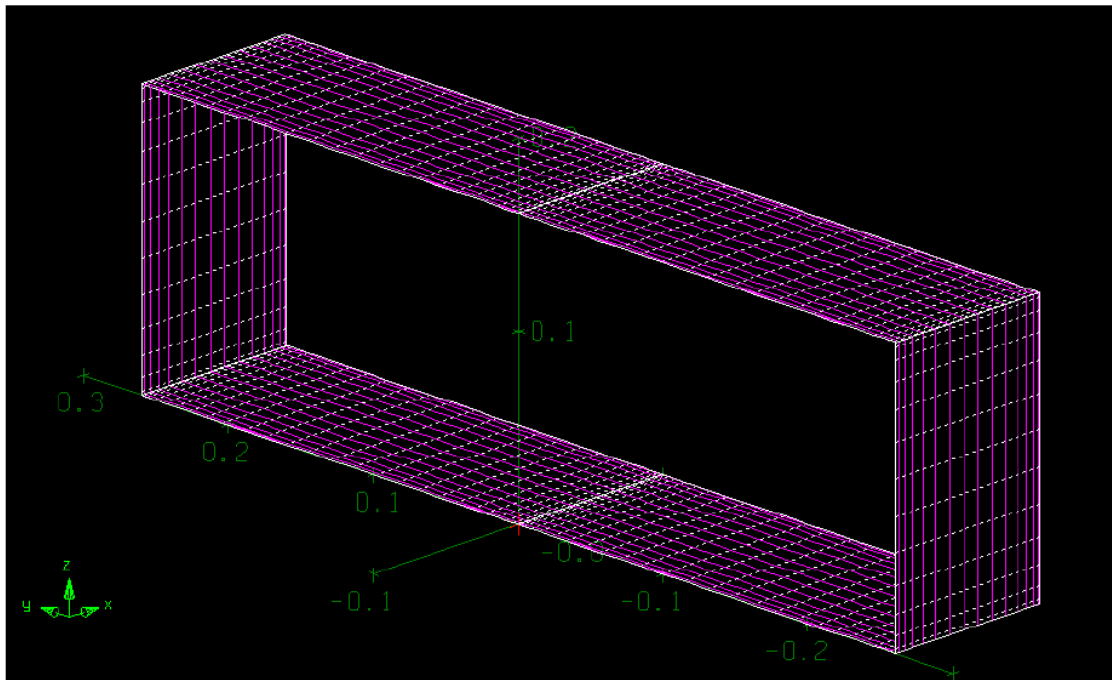
Absolute drag not representative !

Bikkannavar (HAW Hamburg)

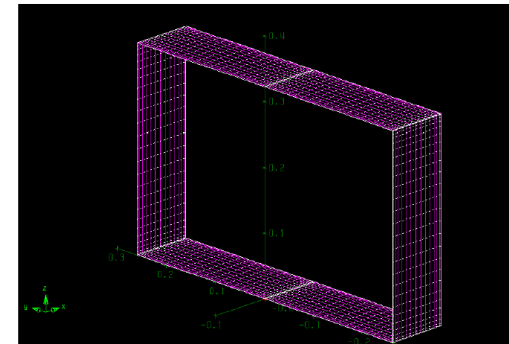
Vortex Lattice Method (VLM) and Comparison with Measurements

Vortex Lattice Method

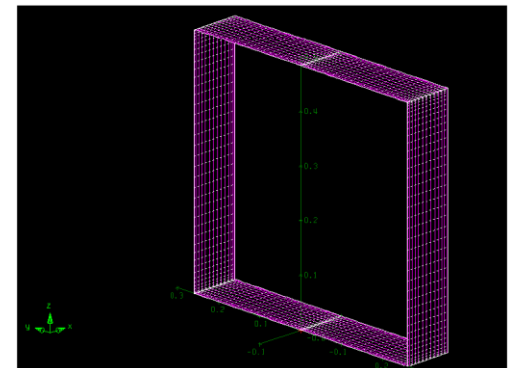
Athena Vortex Lattice (AVL)



$h/b = 0.31$



$h/b = 0.62$

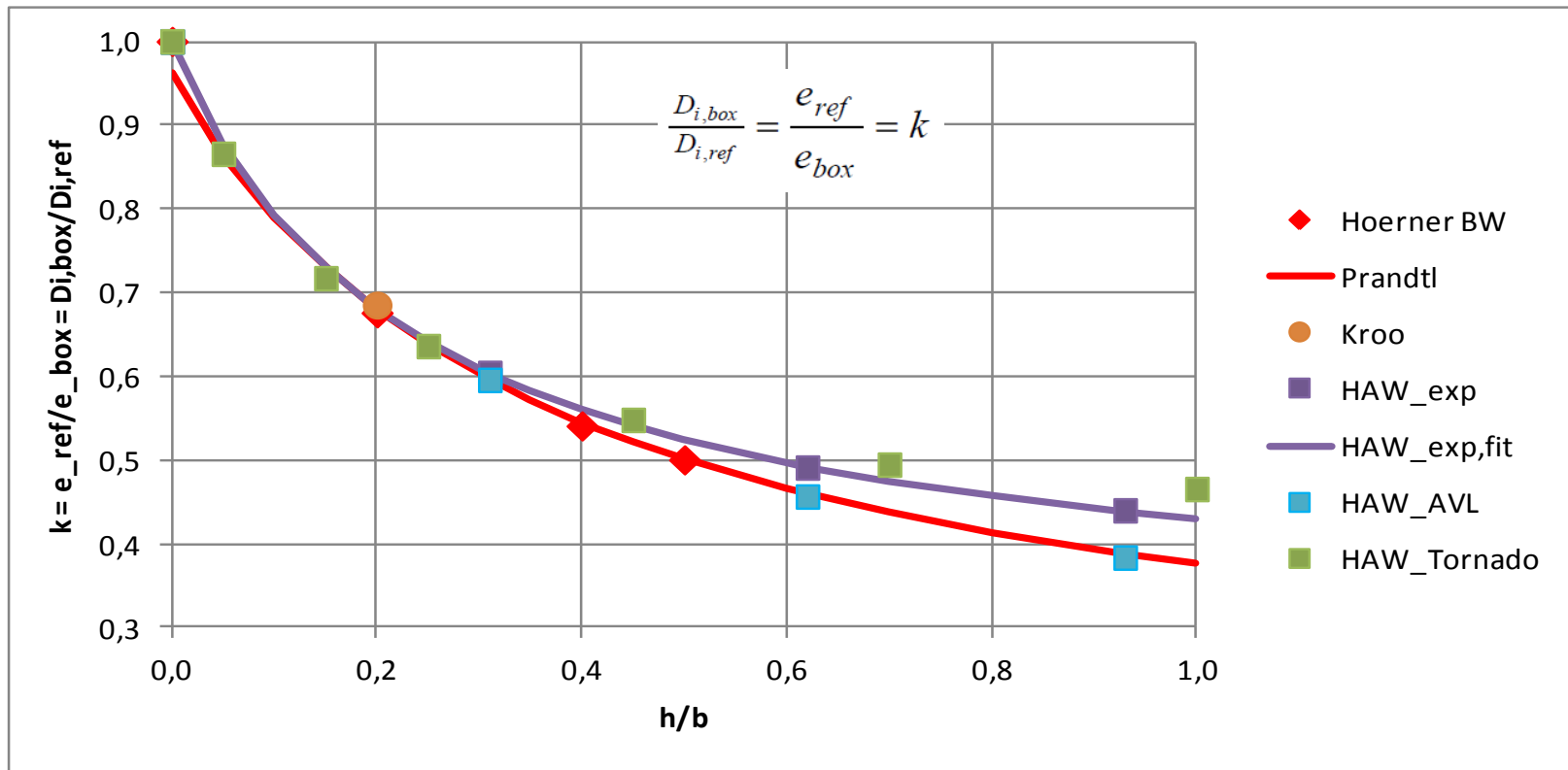


$h/b = 0.93$

Ribeiro (HAW Hamburg)

Comparison: Literature, Wind Tunnel, VLM

Final Result for Box Wing Induced Drag



- HAW_exp: Similar wind tunnel measurements by Fekete, Bikkannavar, Ribeiro. Averaged values.
- HAW_AVL: Ribeiro (HAW Hamburg) using AVL
- HAW_Tornado: Caja Calleja (HAW Hamburg) using Tornado

Comparison: Literature, Wind Tunnel, VLM

Fitting the Wind Tunnel Measurements –

Proposed Equation to Calculate Induced Drag of Box Wings in Conceptual Aircraft Design

$$\frac{D_{i,box}}{D_{i,ref}} = k = \frac{k_1 + k_2 \cdot h/b}{k_3 + k_4 \cdot h/b}$$

box wing equation

$$k_1 = k_3: \quad 0,6952$$

$$k_2: \quad 0,8350$$

$$k_4: \quad 2,8569$$

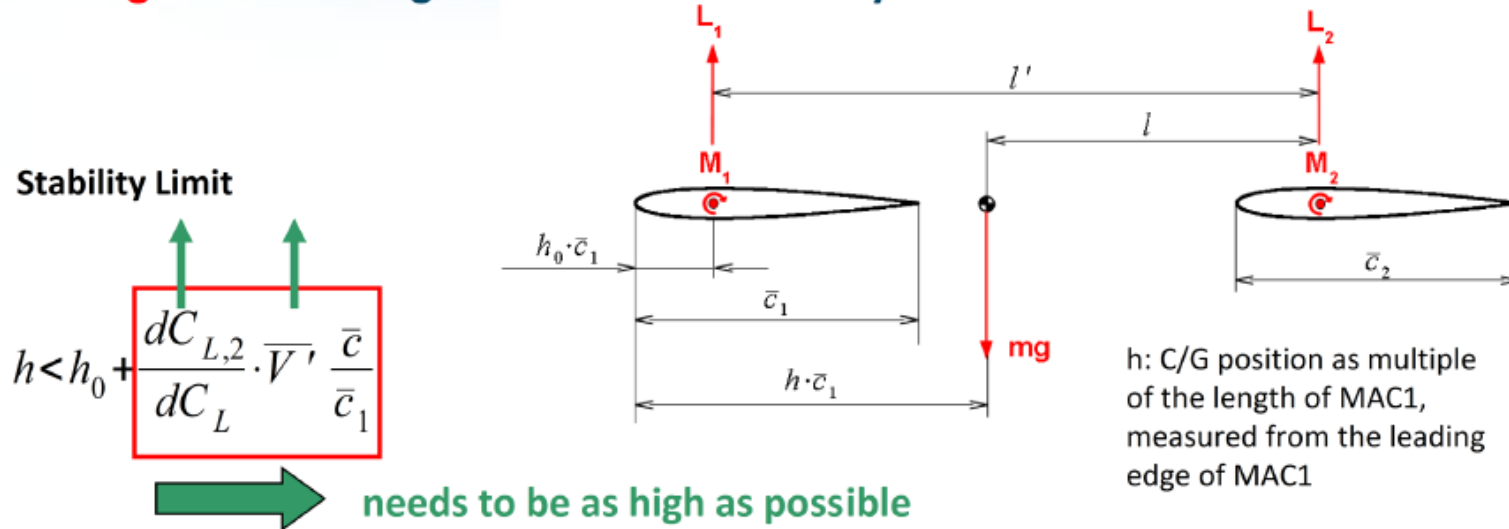
$$h/b \rightarrow \text{infinity}: \quad k_2/k_4 = 0,2923$$

$$h/b = 0: \quad 1,0000$$

- Results from three similar wind tunnel measurement campaigns by Fekete, Bikkannavar, and Ribeiro at HAW Hamburg were averaged.
- Calculations with two VLM – AVL and Tornado – confirmed the measurements.
- **Wind tunnel measurements were fitted to the "box wing equation" (purple curve on previous page) with k-values as given here.**
- The box wing equation compares a box wing and a reference wing with the same aspect ratio $A = b^2/S$, where S is the total wing area.
- The box wing equation was prepared for rectangular and unswept wings.

Induced Drag with Unequal Lift Share

Box Wing Aircraft: Longitudinal Static Stability



SCHIKTANZ, D.; SCHOLZ, D.: The Conflict of Aerodynamic Efficiency and Static Longitudinal Stability of Box Wing Aircraft. Venice, CEAS 2011

Schiktanz 2011

- Control Limit → $C_{L,2}$ needs to be low. Thus for a given C_L
 $C_{L,1}$ needs to be increased
- Trim Condition → $C_{L,2}$ needs to be lower than $C_{L,1} \Rightarrow C_{L,1} / C_{L,2} > 1$

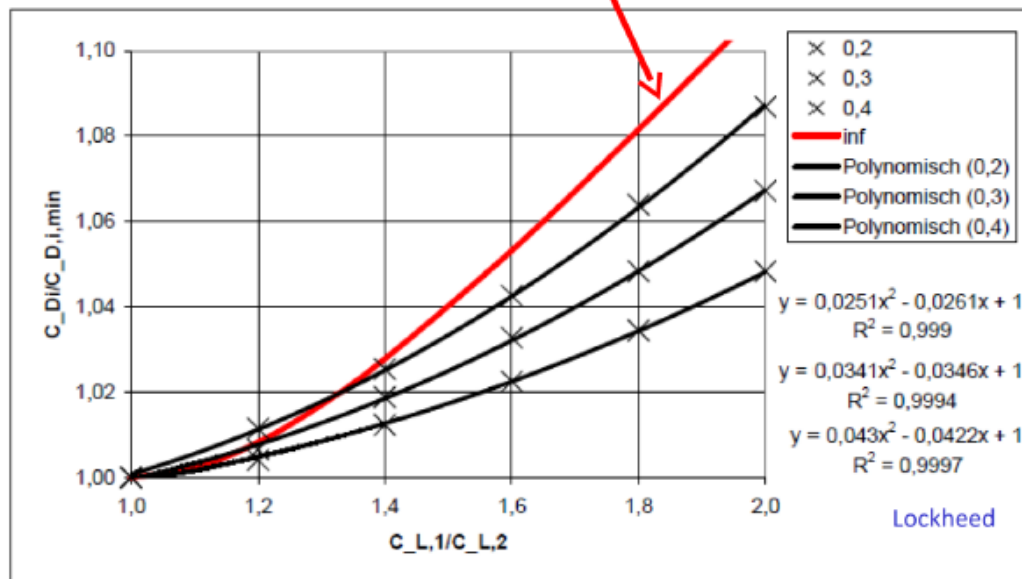
Forward wing needs higher lift coefficient than aft wing

Munk: drag independant of stagger

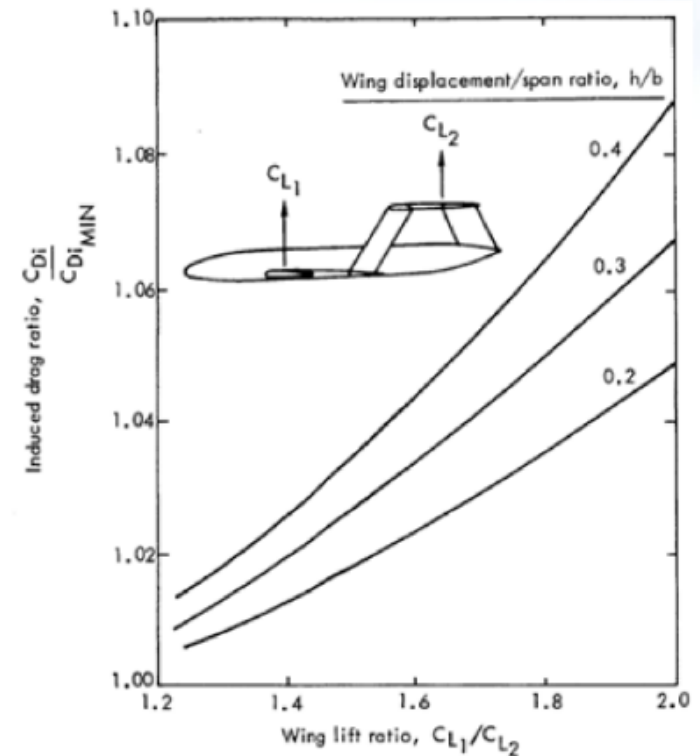
Box Wing Aircraft: Aerodynamics

Prandtl (for $h/b = \text{infinity}$):

$$\frac{C_{D,i}}{C_{D,i,min}} = \frac{2(x^2 + 1)}{(x + 1)^2} \quad \text{with} \quad x = \frac{C_{L,1}}{C_{L,2}}$$



LOCKHEED: Transonic Biplane Concepts.
NACA CR 132462, 1974

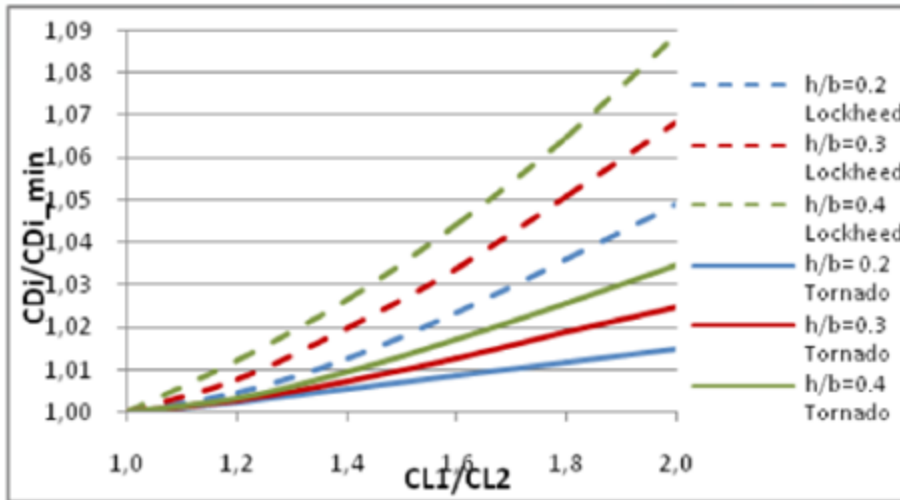


Lockheed 1974

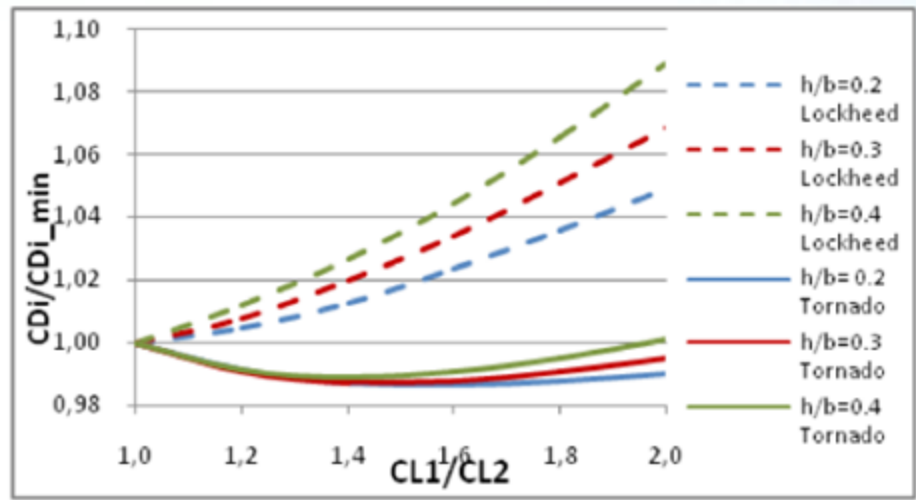
Induced drag increases if lift coefficients are different

Box Wing Aircraft: Aerodynamics

Ricardo Caja Calleja (HAW Hamburg)

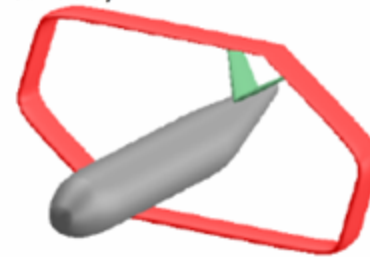
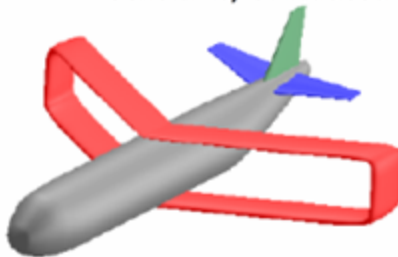


Stagger = 0



Stagger = -0.5b

Sensitivity of induced drag to non-optimum lift distributions (Tornado)



If forward wing is low wing: no drag increase

Summary

Induced Drag Estimation of Box Wings for Conceptual Aircraft Design

Summary

- Common for passenger aircraft is a Box Wing Aircraft (BWA) with **negative stagger**: The forward wing is the low wing. As such the aft wing can use the vertical tail structure for **highest h/b ratio**.
- This configuration could use slight positive decalage (more angle of attack on the upper wing) to adapt the upper wing to the downwash from the front wing.
- However: **Positive decalage can lead to separation already at lower angle of attack and hence reduced maximum lift coefficient**. A conservative design should do without decalage.
- An **unequal lift share** (between forward and aft wing) – as required by static longitudinal stability – **does not necessarily lead to increased induced drag** at (typical) negative stagger.
- Wind tunnel measurements and Vortex Lattice Method (VLM) calculations lead to a **proposal of "k-values" for the "box wing equation" not far from Prandtl's results**. This is straight advice to calculate induced drag of box wings for the conceptual aircraft design phase.

Induced Drag Estimation of Box Wings for Conceptual Aircraft Design

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